

$$\int \frac{dx}{x-a}$$

$$S(dx/(x-a))=S(d(x-a)/(x-a))=S(dt/t)=\ln|x-a|+C$$

$x-a=t$

$$dx=d(x-a)=dx-da=dx-0$$

$$\int \frac{dx}{(x-a)^k}$$

$$S(dx/(x-a)^k)=S(d(x-a)/(x-a)^k)=$$
$$=S(dt/t^k)=t^{-(k-1)}/(1-k)+C=(x-a)^{-(k-1)}/(1-k)+C$$

$$\int \sin mx \, dx$$

$(m \neq 0)$

$$S(\sin(mx))dx=1/m \cdot S(\sin(mx))d(mx)=$$
$$=1/m \cdot S(\sin(t))d(t)=1/m(-\cos t)+C=$$
$$-\cos mx/m+C$$

$$\int \cos mx \, dx$$

$$S(\cos(mx))dx=1/m S(\cos(mx))/d(mx))=$$
$$=1/m S(\cos t/dt)=1/m(\sin t)+C=$$
$$=\sin mx/m+C$$

$$dx^2=2x dx$$

$$dx^2/dx=2x$$

$$(x^2)'=2x$$

$$d(x^2)/dx=2x$$

$$\int e^{-3x} dx$$

$$S(e^{-3x})dx=-1/3 S(e^{-3x})d(-3x)=$$
$$-1/3 S(e^{-t})d(t)=-1/3 e^{-3x}+C$$

$$\int \frac{dx}{\sqrt{a^2-x^2}}$$

$$S(dx/\sqrt{a^2-x^2})=1/a \cdot S(d(ax)/\sqrt{a^2-x^2})=$$
$$=1/a \cdot S(d(x)/\sqrt{[a^2-x^2]/a^2})=$$
$$=1/a \cdot S(d(x)/\sqrt{1-(x/a)^2})=$$
$$=a/a \cdot S(d(x/a)/\sqrt{1-(x/a)^2})=$$
$$=S(dt/\sqrt{1-t^2})=\arcsin t+C=\arcsin(x/a)+C$$

$$\int \frac{dx}{a^2+x^2}$$

$$S(dx/(a^2+x^2))=1/a^2 \cdot S(d(a^2x)/(a^2+x^2))=$$
$$=1/a^2 \cdot S(d(x)/(a^2+x^2)/a^2)=$$
$$=1/a^2 \cdot S(d(x)/(1+(x/a)^2))=$$
$$=a/a^2 \cdot S(d(x/a)/(1+(x/a)^2))=$$
$$=1/a \cdot S(dt/(1+t^2))=$$
$$=1/a \cdot \arctg(t)+C=1/a \cdot \arctg(x/a)+C$$

$$\int \frac{(e^x-1)(e^{2x}+1)}{e^x} dx$$

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