

$$\int \cos^2 mx \, dx$$

$$\begin{aligned} \int (\cos^2(mx)) dx &= \int \left(\frac{1 + \cos 2mx}{2} \right) dx = \int \left(\frac{1}{2} \right) dx + \int \left(\frac{\cos 2mx}{2} \right) dx = \\ &= \frac{x}{2} + \frac{1}{2} \int \cos 2mx \, dx = \frac{x}{2} + \frac{1}{2} \int \cos 2mx / 2m \, d(2mx) = \\ &= \frac{x}{2} + \frac{\sin 2mx}{4m} + C \end{aligned}$$

$$\int \sin^2 mx \, dx$$

$$\begin{aligned} \int (\sin^2(mx)) dx &= \int \left(\frac{1 - \cos 2mx}{2} \right) dx = \int \left(\frac{1}{2} \right) dx - \int \left(\frac{\cos 2mx}{2} \right) dx = \\ &= \frac{x}{2} - \frac{1}{2} \int \cos 2mx \, dx = \frac{x}{2} - \frac{1}{2} \int \cos 2mx / 2m \, d(2mx) = \\ &= \frac{x}{2} - \frac{\sin 2mx}{4m} + C \end{aligned}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$