

$$(a) \int \ln x \, dx,$$

$$\int \ln x \, dx = x \ln x - \int x dx / x = x \ln x - \int dx = x \ln x - x$$

$$(b) \int \arctg x \, dx$$

$$u = \ln x$$

$$dv = dx$$

$$(B) \int \arcsin x \, dx$$

$$v = x$$

$$du = dx/x$$

$$\int (\arcsin x) dx =$$

$$= x \arcsin x - \int x dx / \sqrt{1-x^2} =$$

$$= x \arcsin x + \frac{1}{2} \int d(-x^2) / \sqrt{1-x^2} =$$

$$= x \arcsin x + \frac{1}{2} \int d(1-x^2) / \sqrt{1-x^2} =$$

$$= [t = 1-x^2] = x \arcsin x + \frac{1}{2} \int t^{-1/2} dt =$$

$$= x \arcsin x + \frac{1}{2} \cdot \sqrt{t} / (1/2) = x \arcsin x + \sqrt{1-x^2} + C$$

$$u = \arcsin x$$

$$dv = dx$$

$$v = x$$

$$du = dx / \sqrt{1-x^2}$$

$$\int u \, dv = uv - \int v \, du$$

$$\int (\arctg x) dx = x \arctg x - \int x / (1+x^2) =$$

$$= x \arctg x - \int x dx / (1+x^2) =$$

$$= x \arctg x - \frac{1}{2} \int d(1+x^2) / (1+x^2) = [t = 1+x^2] =$$

$$= x \arctg x - \frac{1}{2} \int dt / t = x \arctg x - \frac{1}{2} \ln |t| + C =$$

$$x \arctg x - \frac{1}{2} \ln(1+x^2) + C$$

$$u = \arctg x$$

$$dv = dx$$

$$v = x$$

$$du = dx / (1+x^2)$$