

$$(a) \int \ln x \, dx,$$

2)

$$\begin{aligned} S(\arctg x) \, dx &= \arctg x \cdot x - S(x/(1+x^2)) \, dx = x \arctg x - S(d(x^2/2)/(1+x^2)) = \\ &= x \arctg x - \frac{1}{2} S(d(x^2)/(1+x^2)) = x \arctg x - \frac{1}{2} S(d(t)/(1+t)) = \\ &= x \arctg x - \frac{1}{2} S(d(t+1)/(1+t)) = x \arctg x - \frac{1}{2} S(dz/z) = x \arctg x - \frac{1}{2} \ln z + C = \\ &= x \arctg x - \frac{1}{2} \ln(t+1) + C = x \arctg x - \frac{1}{2} \ln(x^2+1) + C \end{aligned}$$

$$(b) \int \arcsin x \, dx$$

$$u = \arctg x$$

$$du = 1/(1+x^2)$$

$$dv = dx$$

$$v = x$$

$$x \, dx = d(x^2/2)$$

$$x^2 = t$$

$$t+1 = z$$

$$dt = d(t+1)$$

3)

$$S(\arcsin x) \, dx = \arcsin x \cdot x - S(x \, dx / \sqrt{1-x^2}) =$$

$$x \arcsin x - S(d(x^2/2) / \sqrt{1-x^2}) =$$

$$x \arcsin x - \frac{1}{2} S(d(x^2) / \sqrt{1-x^2}) = x \arcsin x - \frac{1}{2} S(d(t) / \sqrt{1-t}) =$$

$$= x \arcsin x - \frac{1}{2} S(d(t) / \sqrt{1-t}) = x \arcsin x + \frac{1}{2} S(d(-t+1) / \sqrt{1-t}) =$$

$$= x \arcsin x + \frac{1}{2} S(d(z) / \sqrt{z}) = x \arcsin x + \frac{1}{2} S(z^{-1/2}) \, dz =$$

$$x \arcsin x + z^{1/2} + C = x \arcsin x + (-t+1)^{1/2} + C =$$

$$x \arcsin x + (-x^2+1)^{1/2} + C = x \arcsin x + \sqrt{1-x^2} + C$$

$$u = \arcsin x$$

$$du = 1/\sqrt{1-x^2} \, dx$$

$$dv = dx$$

$$v = x$$

$$x^2 = t$$

$$-t+1 = z$$