

$$\int x^2 \sin x \, dx$$

$$\begin{aligned} \int (x^2 \sin x) dx &= -x^2 \cos x - \int (-\cos x) 2x dx = \\ &= -x^2 \cos x + 2 \int (x \cos x) dx = \\ &= -x^2 \cos x + 2(x \sin x + \cos x) + C \end{aligned}$$

$$\begin{aligned} u &= x^2 \\ dv &= \sin x dx \\ v &= -\cos x \\ du &= 2x dx \end{aligned}$$

$$\begin{aligned} \int (x \cos x) dx &= x \sin x - \int (\sin x) dx = \\ &= x \sin x + \cos x + C \\ u &= x \\ dv &= \cos x dx \\ v &= \sin x \\ du &= dx \end{aligned}$$

$$\begin{aligned} \int (x^2 \sin x) dx &= \frac{1}{3} \int \sin x \cdot dx^3 = \\ &= x^3 \sin x - \frac{1}{3} \int (x^3 \cos x) dx = \\ &= x^3 \sin x - \frac{1}{3} \int (x^3 \cos x) dx \\ u &= \sin x \\ dv &= dx^3 \\ v &= x^3 \\ du &= \cos x dx \end{aligned}$$

$$\begin{aligned} \int (x^2 \sin x) dx &= x^3 \cos x - \\ &- 2 \int (2x \sin x + x^2 \cos x) dx \\ u &= x^2 \sin x \\ dv &= dx \\ v &= x \\ du &= (2x \sin x + x^2 \cos x) dx \end{aligned}$$