

$$\int x^2 \sin x \, dx$$

$$\begin{aligned} S(x^2 \sin x) dx &= -\cos x \cdot x^2 - S(-\cos x \cdot 2x dx) = -\cos x \cdot x^2 + 2S(\cos x \cdot x dx) = \\ &= -\cos x \cdot x^2 + 2(x \sin x + \cos x + C) = -\cos x \cdot x^2 + 2(x \sin x + \cos x) + 2C \end{aligned}$$

$$x^2 \sin x \, dx + 2(\cos x \cdot x^2 / 2 + S(x^2 / 2 \cdot \sin x dx)) = x^2 \sin x \, dx + (\cos x \cdot x^2 + S(x^2 \cdot \sin x dx))$$

$$u = x^2$$

$$du = 2x dx$$

$$dv = \sin x \, dx$$

$$v = -\cos x$$

$$S(\cos x \cdot x dx) = \cos x \cdot x^2 / 2 + S(x^2 / 2 \cdot \sin x) dx$$

$$u = \cos x$$

$$du = -\sin x dx$$

$$dv = x dx$$

$$v = x^2 / 2$$

$$S(\cos x \cdot x dx) = x \sin x - S(\sin x) dx = x \sin x + \cos x + C$$

$$u = x$$

$$du = dx$$

$$dv = \cos x dx$$

$$v = \sin x$$

$$S(x^2 \sin x) dx = x^3 / 3 \cdot \sin x - S(x^3 / 3) \cos x dx$$

$$u = \sin x$$

$$du = \cos x dx$$

$$dv = x^2 dx$$

$$v = x^3 / 3$$