

Найдите точку максимума функции  $y = (x+6)^2 e^{4-x}$

$$\begin{aligned}y' &= ((x+6)^2 e^{4-x})' = \\ &= 2(x+6)e^{4-x} + (x+6)^2 e^{4-x}(-1) = \\ &= (x+6)e^{4-x} [2 - (x+6)] = \\ &= -(x+6)e^{4-x} [x+4]\end{aligned}$$

$$\begin{aligned}&= -10e^{4-x} - 24e^{4-x} - x^2 e^{4-x} = \\ &= -e^{4-x}(10x+24+x^2) \\ &-e^{4-x}(10x+24+x^2) = 0 \\ &e^{4-x}(10x+24+x^2) = 0 \\ &e^{4-x} = 0 \quad 10x+24+x^2 = 0 \\ &x \in \mathbb{R} \quad x = -6 \quad x = -4 \\ &x = -6 \quad x = -4 \\ &x_{\max} = -4\end{aligned}$$

