

15. Given  $z = 1 - 2i$  is a root of  $p(z) = z^4 + 9z^3 - 2z^2 - 8z + 20$ , factorise the polynomial  $p$  fully over  $\mathbb{C}$ .

$$(z-1-2i)(z-1+2i) = z^2 - z + 2zi - z + 1 - 2i - 2zi + 2i - 4i^2 =$$

$$= z^2 - 2z + 5$$

$$\begin{array}{r|l} z^4 + 9z^3 - 2z^2 - 8z + 20 & z^2 - 2z + 5 \\ z^4 - 2z^3 + 5z^2 & z^2 + 11z + 15 \end{array}$$

$$11z^3 - 7z^2 - 8z$$

$$11z^3 - 22z^2 + 55z$$

$$15z^2 - 63z + 20$$

$$15z^2 - 30z + 75$$