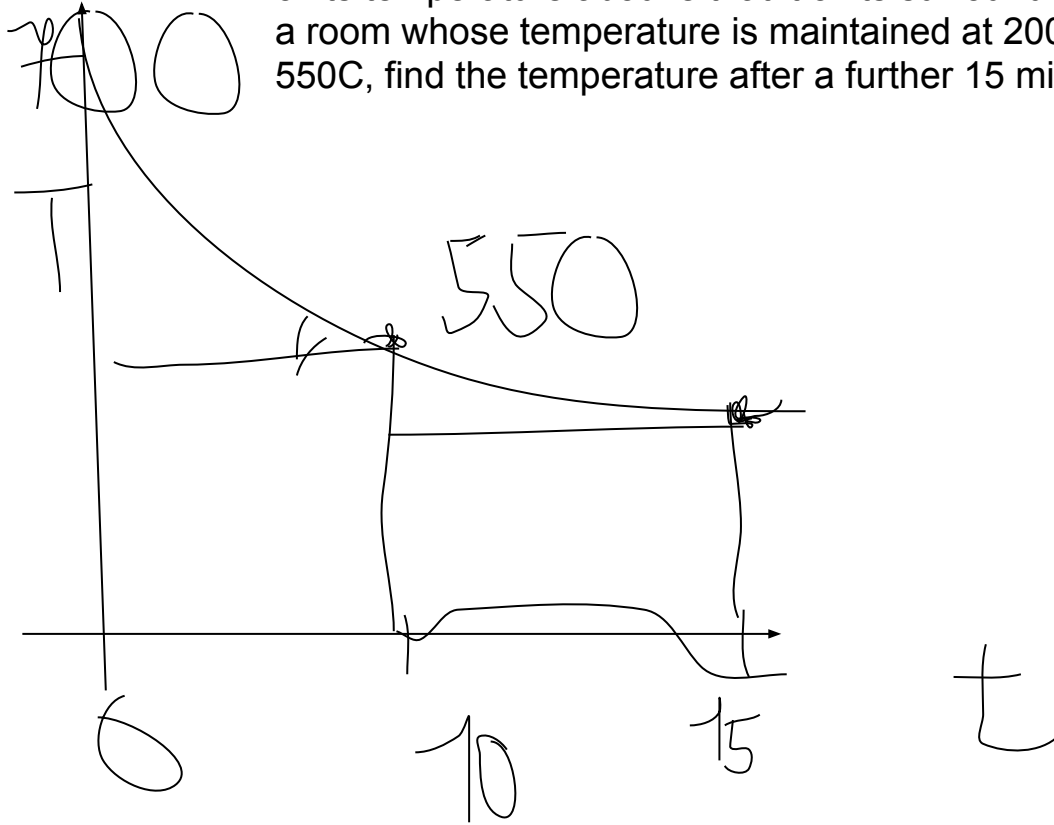


Newton's Law of cooling states that the rate of cooling of a body is proportional to the excess of its temperature above that of its surroundings. A body at a temperature 700C is placed in a room whose temperature is maintained at 200C. If, after 10 min, the temperature of the body is 550C, find the temperature after a further 15 min.



Newton's Law of Cooling

$$T(t) = T_s + (T_0 - T_s)e^{-kt}$$

$$\frac{dT}{dt} = -k(T - T_s)$$

$$T(t) = T_s + (T_0 - T_s)e^{-kt}$$

$$T'(t) = -k(T_0 - T_s)e^{-kt}$$

$$dT/dt = -k(T - T_s)$$

$$1/(T - T_s)dT = -kdt$$

$$\int 1/(T - T_s)dT = \int -kdt$$

$$\ln|T - T_s| = -kt + C$$

$$\ln|700 - 550| = 0 + C$$

$$C = \ln|150|$$

$$\ln|550 - T_s| = -15k + \ln|150|$$

$$e^{\ln|550 - T_s|} = e^{(-15k + \ln|150|)}$$

$$T_s = -e^{(-15k + \ln|150|)} + 550$$