

Determine whether the following improper integrals converge.

$$\text{i) } \int_2^{+\infty} \frac{dx}{\sqrt[5]{3x^6 + 4}}$$

$$\text{ii) } \int_0^1 \frac{dx}{3 - 2x\sqrt[3]{x}}$$

$$\int_2^{+\infty} \frac{dx}{\sqrt[5]{3x^6 + 4}} < \int_2^{+\infty} \frac{dx}{x^{6/5}}$$

$$\int_2^{+\infty} \frac{dx}{x^{6/5}} = \lim_{b \rightarrow +\infty} \left[-5x^{-1/5} \right]_2^b = -5b^{-1/5} + 5 \cdot 2^{-1/5} = 5 \cdot 2^{-1/5}$$

$$\frac{1}{\sqrt[5]{3-2x^6}} > \frac{1}{3-2x} > \frac{1}{3-3x}$$

$$\int \frac{1}{3-2x} dx = \ln|3-2x| \Big|_1^b = \ln|1| - \ln|3-2b| \Rightarrow$$

$$\frac{1}{3-2x^2} > \frac{1}{\sqrt[5]{3-2x^6}}$$

$$\int \frac{dx}{3-2x^2} =$$

$$\frac{1}{3-2x^2} = \frac{a}{\sqrt{3-2x}} + \frac{b}{\sqrt{3+2x}}$$