

$P(x) / 1 \rightarrow \infty$ Euclid
(prime numbers are infinite)

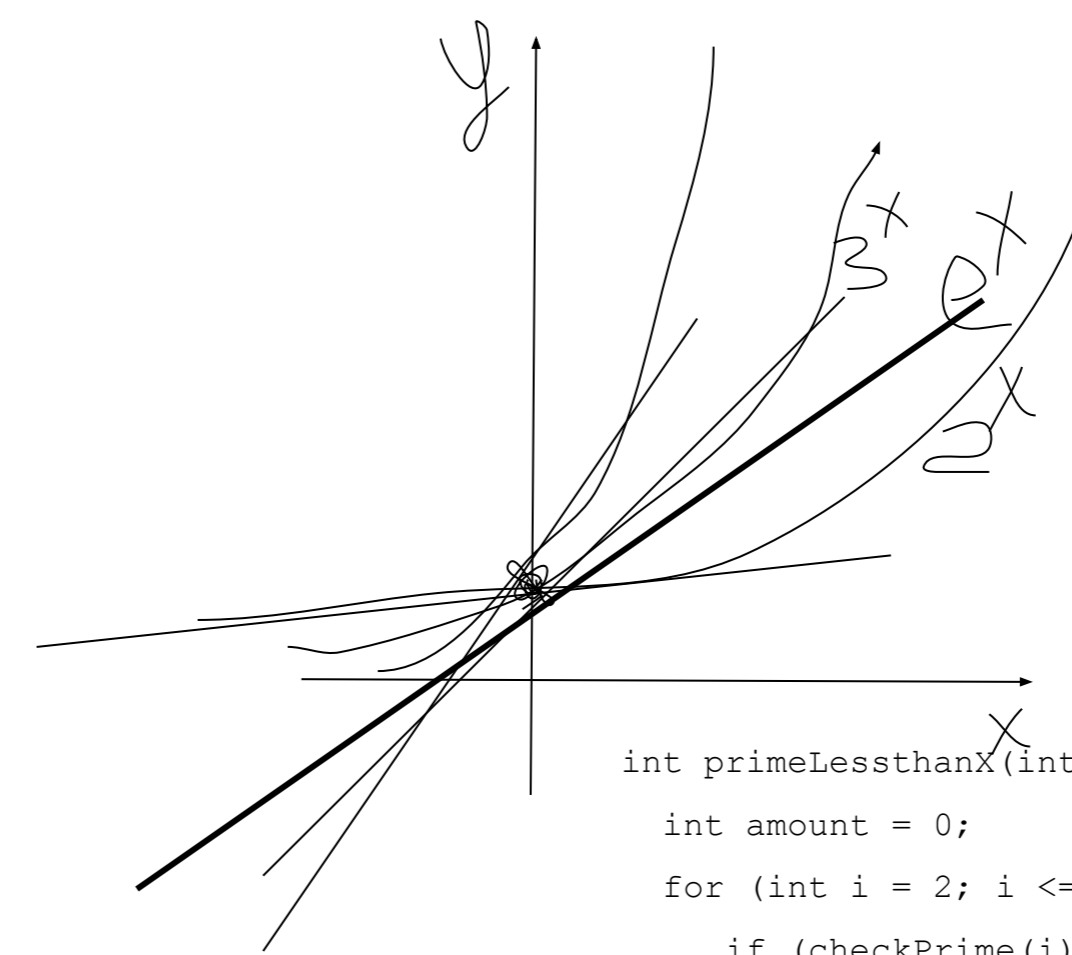
$P(x) / x \rightarrow 0$ $x \rightarrow \infty$
(XVIII - Leonard Euler)

$P(x) / x/\ln(x) \rightarrow 1$
(XIX Chebyshev) $e=2,71\dots$

Distribution of primes

$P(n)$ - amount of primes less than n
 $P(20)=[3,5,7,11,13,17,19]=7$

$x=1000000$
 $x/\ln(x)=1000000/\ln(1000000)$



$$\log_a(b) = \frac{\log_c(b)}{\log_c(a)}$$

$$\log_e(b) = \frac{\log_c(b)}{\log_c(e)}$$

```
int primeLessthanX(int number) {
    int amount = 0;
    for (int i = 2; i <= number; i++) {
        if (checkPrime(i) == 1) {
            amount++;
            //std::cout << i << std::endl;
        }
    }
    std::cout << amount << std::endl;
    return amount;
}
```

```
int number = 20000000;
```

```
int pX = primeLessthanX(number);
int pY = (double)number / log(number);
std::cout << pY << std::endl;
std::cout << ((double)pY / (double)pX) * 100 << std::endl;
```

Bertrand's postulate (there is at least one prime number between n and $2n$)

$$x/\ln(x) \sim P(x)$$

$$2x/\ln(2x) \sim P(2x)$$

$$P(2x) - P(x) = 2x/\ln(2x) - x/\ln(x) =$$

$$= x[2/\ln(2x) - 1/\ln(x)] > x[2/\ln(2x) - 1/\ln(2x)] = x[1/\ln(2x)] = x/\ln(2x) > 1$$