

(!!!)Квадрат суммы и разности (разложить на множители методом группировки)

$$1) x^2 + 2xy + y^2 = x^2 + xy + xy + y^2 = x(x+y) + y(x+y) = (x+y)(x+y) = (x+y)^2$$

$$x^2 + 2xy + y^2 = (x+y)^2 \text{ **Квадрат суммы**}$$

$$(x+y)^2 = (x+y)(x+y) = (x+y) * x + (x+y) * y = x*x + x*y + y*x + y*y = x^2 + y^2 + xy + yx = x^2 + y^2 + xy(1+1) = x^2 + y^2 + 2xy$$

$$2) x^2 - 2xy + y^2 = x^2 - (xy + xy) + y^2 = x^2 - xy - xy + y^2 = x(x-y) + y(-x+y) = -x(-x+y) + y(-x+y) = (-x+y)(-x+y) = (-x+y)^2 = (x-y)^2$$

$$x^2 - 2xy + y^2 = (x-y)^2 \text{ **Квадрат разности**}$$

$$(x-y)^2 = (x-y)(x-y) = (x-y)*x + (x-y)*(-y) = x*x - x*y + (-y)*x + y*y = x^2 - xy - yx + y^2 = x^2 + xy(-1-1) + y^2 = x^2 - 2xy + y^2$$

$$x-y = x + (-1)*y$$

$$3) a^2 + b^2 + c^2 + 2ab + 2ac + 2bc = a^2 + b^2 + c^2 + ab + ab + ac + ac + bc + bc = a(a+b+c) + b(b+a+c) + c(c+a+b) = (a+b+c)(a+b+c) = (a+b+c)^2$$

$$a^2 + b^2 + c^2 + 2ab + 2ac + 2bc = (a+b+c)^2$$

**Квадрат суммы трех слагаемых**

$$(a+b+c)^2 = (a+b+c)(a+b+c) = (a+b+c)*a + (a+b+c)*b + (a+b+c)*c = a*a + a*b + a*c + b*a + b*b + b*c + c*a + c*b + c*c = a^2 + ab + ac + ba + b^2 + bc + ca + cb + c^2 = a^2 + 2ab + 2ac + 2cb + b^2 + c^2$$

$$4) a^2 + b^2 + c^2 - 2ab + 2ac - 2bc = a^2 + b^2 + c^2 - ab - ab + ac + ac - bc - bc = a(a-b+c) + b(b-a-c) + c(c+a-b) = a(a-b+c) - b(-b+a+c) + c(c+a-b) = (a-b+c)(a-b+c) = (a-b+c)^2$$

$$(a-b-c)^2 = (a + (-b) + (-c))^2 = a^2 + (-b)^2 + (-c)^2 + 2a(-b) + 2a(-c) + 2(-b)(-c) = a^2 + b^2 + c^2 - 2ab - 2ac + 2bc$$

$$a*(b+c) = ab + ac$$

$$a+a = a(1+1) = 2a$$

$$(a+b)(c+d)$$

$$(a+b)^2$$

$$2xy = xy + xy$$

$$2a = a + a$$

$$-(a+b) = (-1)(a+b) =$$

$$(-1)*a + (-1)*b = -a - b$$

$$-(-a+b) = (-1)*(-a+b) =$$

$$(-1)*(-a) + (-1)*b =$$

$$= a - b$$

$$[-x+y]^2 = [(-1)*x + (-1)(-1)*y]^2 =$$

$$=[(-1) * (x + (-1)*y)]^2 =$$

$$=[(-1) * (x-y)]^2 = (-1)^2 * (x-y)^2 =$$

$$= (x-y)^2$$

$$(-x+y)^2 = (x-y)^2$$

$$[-(x-y)]^2$$

$$(ab)^2 = a^2 * b^2$$

ДЗ

Разложить на множители

$$1) a^2 + 4ab + 4b^2 = a^2 + 2ab + 2ab + 4b^2 = a(a+2b) + 2b(a+2b) = (a+2b)(a+2b) = (a+2b)^2$$

$$2) x^2 - 5xy + 6y^2 = x^2 - 2xy - 3xy + 6y^2 = x(x-2y) - 3y(x-2y) = (x-2y)(x-3y)$$

найти значение выражения при  $x=10001$  и  $y=19$

$$(x^2 - 5xy + 6y^2) / (x-2y) = (x-2y)(x-3y) / (x-2y) = (x-3y) = 10001 - 19*3$$