

Куб суммы и разности (разложить на множители методом группировки)

$$x^2 + xy + xy + y^2 = x(x+y) + y(y+x) = (x+y)(x+y)$$

$$x^2 - xy - xy + y^2 = x(x-y) - y(-y+x) = (x-y)(x-y) = (x-y)^2$$

$$\begin{aligned} 1)(!!!) \quad & x^3 + 3x^2y + 3y^2x + y^3 = \\ & = x^3 + x^2y + x^2y + x^2y + y^2x + y^2x + y^2x + y^3 = \\ & = x(x^2 + xy + xy + y^2) + y(y^2 + xy + xy + x^2) = \\ & = (x+y)(x^2 + xy + xy + y^2) = (x+y)(x+y)(x+y) = (x+y)^3 \end{aligned}$$

$$\begin{aligned} 2)(!!!) \quad & x^3 - 3x^2y + 3xy^2 - y^3 = \\ & = x^3 - x^2y - x^2y - x^2y + xy^2 + xy^2 + xy^2 - y^3 = \\ & = x(x^2 - xy - xy + y^2) - y(y^2 - xy - xy + x^2) = \\ & = (x-y)(x^2 - xy - xy + y^2) = (x-y)(x-y)^2 = (x-y)^3 \end{aligned}$$

$$(x+y)^3 = x^3 + 3x^2y + 3y^2x + y^3$$

$$(x-y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

