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МФТИ физ-тех

$$\begin{aligned} & (x + y + z)^3 - x^3 - y^3 - z^3 = \\ & (x+y+z-x) \left((x+y+z)^2 + (x+y+z)x + x^2 \right) \\ & - y^3 - z^3 = \\ & (y+z) (2xy + 2yz + 2zx + x^2 + z^2 + y^2 \\ & + x^2 + yx + zx + x^2) - y^3 - z^3 = \\ & (y+z) (2xy + 2yz + 2zx + x^2 + z^2 + y^2 \\ & + x^2 + yx + zx + x^2) - (y^3 + z^3) = \\ & (y+z) * (3xy + 2yz + 3zx + z^2 + y^2 + 3x^2) - \\ & - (y+z) * (y^2 - yz + z^2) = \\ & (y+z) \{ (3xy + 2yz + 3zx + z^2 + y^2 \\ & + 3x^2) - (y^2 - yz + z^2) \} = \\ & (y+z) \{ 3xy + 2yz + 3zx + z^2 + y^2 \\ & + 3x^2 - y^2 + yz - z^2 \} = \\ & (y+z) \{ 3xy + 3yz + 3zx + 3x^2 \} = \\ & (y+z) 3 (xy + yz + zx + x^2) = \\ & 3 (y+z) \{ x (y+x) + z (y+x) \} = 3 (y+z) (x+y) (x+z) \end{aligned}$$

$$\begin{aligned} x^3 + y^3 &= (x+y) (x^2 - xy + y^2) \\ x^3 - y^3 &= (x-y) (x^2 + xy + y^2) \\ (x+y)^3 &= x^3 + 3x^2y + 3xy^2 + y^3 \\ (x-y)^3 &= x^3 - 3x^2y + 3xy^2 - y^3 \\ (x+y)^2 &= x^2 + 2xy + y^2 \end{aligned}$$

$$\begin{aligned} (x+y+z)^2 &= \\ &= (x+y+z) (x+y+z) = \\ &= (x+y+z) * x + (x+y+z) * y \\ &+ (x+y+z) * z = x^2 + x^2 + x^2 + x \\ &* y + x * y + y^2 + y^2 + y^2 + y * z \\ &+ z * x + z * x + z * x + z^2 + z^2 + z^2 \\ &+ yz + yz + yz + zx + zx + zx = xy (\\ &1+1) + yz (1+1) + zx (1+1) \\ &+ x^2 + y^2 + z^2 = \\ &2xy + 2yz + 2zx + x^2 + z^2 + \\ &y^2 \end{aligned}$$