

$$x^2 + 2xy + y^2 = x^2 + xy + xy + y^2 = x(x+y) + y(x+y) = (x+y)(x+y) = (x+y)^2$$

$$4a^2 + 4ab + b^2 = 4a^2 + 2ab + 2ab + b^2 = 2a(2a+b) + b(2a+b) = (2a+b)(2a+b) = (2a+b)^2$$

$$x^2 - 5x + 6 = x^2 - 2x - 3x + 6 = x(x-2) - 3(x-2) = (x-2)(x-3)$$

$$x^2 + 5x - 6 = x^2 + 2x + 3x - 6 = x(x+2) + 3(x-2)$$

$$x^2 + 5x - 6 = x^2 + 6x - x - 6 = x^2 - x + 6x - 6 = x(x-1) + 6(x-1) = (x-1)(x+6)$$

$$2x^2 - 5x + 3 = 2x^2 - 2x - 3x + 3 = 2x(x-1) - 3(x-1) = (x-1)(2x-3)$$

$$35a^2 + 2ab - b^2 = 35a^2 - 5ab + 7ab - b^2 = 5a(7a-b) + b(7a-b) = (7a-b)(5a+b)$$

$$10a^2 + 9ab - 9b^2 = 10a^2 - 1ab + 10ab - 9b^2 = 10a(a+b) - b(a+9b)$$

$$10a^2 - 3ab + 12ab - 9b^2 = 10a^2 + 12ab - 3ab - 9b^2 = 2a(5a+6b) - 3b(a+3b)$$

$$\begin{aligned} 10a^2 - 6ab + 15ab - 9b^2 &= 10a^2 + 15ab - 6ab - 9b^2 \\ &= 5a(2a+3b) - 3b(2a+3b) = (2a+3b)(5a-3b) \end{aligned}$$

$$\begin{aligned} a^2 + 2bc + b^2 + c^2 + 2ab + 2ac &= a^2 + 2ab + 2ac + 2bc + b^2 + c^2 = \\ &= a(a+2b+2c) + b(2c+b+c^2) \end{aligned}$$

$$a^2 + bc + bc + b^2 + c^2 + ab + ab + ac + ac =$$

$$\begin{aligned} a^2 + ab + ac + bc + b^2 + 2ab + bc + ac + c^2 &= a(a+b+c) + b(c+b+a) + c(b+a+c) = \\ (a+b+c)(a+b+c) &= (a+b+c)^2 \end{aligned}$$

$$4a^2 + 9b^2 + c^2 + 12ab - 6bc - 4ac = 4a^2 + 9b^2 + c^2 + 6ab + 6ab - 3bc - 3bc - 2ac - 2ac =$$

$$4a^2 + 6ab - 2ac + 9b^2 + 6ab - 3bc + c^2 - 3bc - 2ac$$

$$= 2a(2a+3b-c) + 3b(3b+2a-c) - c(-c+3b+2a) = (2a+3b-c)(2a+3b-c) = (2a+3b-c)^2$$