

Разбиение отдельных членов на слагаемые (как буквенных, так и числовых)

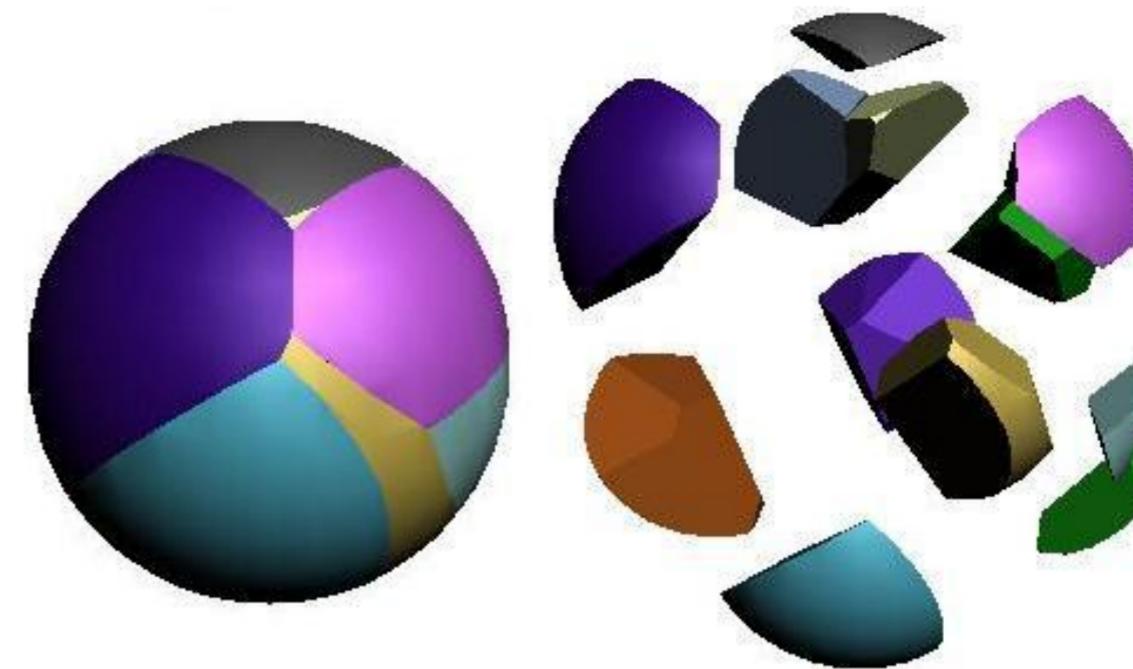
1) $x^3 + 1991x + 1992 = 0$

2) $x^3 - 3x^2 + 2 = 0$

3) $x^4 - x^3 - 13x^2 + x + 12 = 0$

4) $x^3 + 4x^2 - 5 = 0$

5) $x^4 - x^3 - 7x^2 + x + 6 = 0$



$x^3 + 1991x + 1992 = 0;$
 $x^3 + 1991x + 1991 + 1 = 0;$
 $(x^3 + 1) + 1991(x + 1) = 0;$
 $(x + 1)(x^2 - x + 1) + 1991(x + 1) = 0;$
 $(x + 1)((x^2 - x + 1) + 1991) = 0;$
 $(x + 1)(x^2 - x + 1992) = 0;$
 $x_1 = -1$
 $x^2 - x + 1992 = 0;$
 $D = 1 - 4 * 1992 < 0; D < 0;$
no solutions

Answer: -1;

$x^3 + 1992x - x + 1992 = 0;$
 $x^3 - x + 1992x + 1992 = 0;$
 $x(x^2 - 1) + 1992(x + 1) = 0;$
 $x(x - 1)(x + 1) + 1992(x - 1) = 0;$
 $(x + 1)(x(x - 1) + 1992) = 0;$
 $x_1 = -1$

$(x^2 - x + 1992) = 0;$
 $D = 1 - 4 * 1992 < 0; D < 0$
no solutions

Answer: -1;

$$\begin{aligned} x^3 - 3x^2 + 2 &= 0; \\ x^3 - 2x^2 - x^2 + 2 &= 0; \\ x^3 - x^2 - 2x^2 + 2 &= 0; \\ x^2(x - 1) - 2(x^2 - 1) &= 0; \\ x^2(x - 1) - 2(x - 1)(x + 1) &= 0; \\ (x - 1)(x^2 - 2(x + 1)) &= 0; \\ x_1 &= 1; \end{aligned}$$

$$\begin{aligned} x^2 - 2x - 2 &= 0 \\ D = 4 + 8 &= 12; D > 0; \\ x_2 = (2 - V12)/2 &= 2 - 2V3/2 = 1 - V3; \\ x_3 = (2 + V12)/2 &= 2 + 2V3/2 = 1 + V3; \end{aligned}$$

Answer: 1; 1 - V3; 1 + V3;

$$\begin{aligned} x^4 - x^3 - 7x^2 + x + 6 &= 0; \\ x^4 - x^3 - 6x^2 + 6 - x^2 + x &= 0; \\ x^3(x - 1) - 6(x^2 - 1) - x(x - 1) &= 0; \\ x^3(x - 1) - 6(x - 1)(x + 1) - x(x - 1) &= 0; \\ (x - 1)(x^3 - 6(x + 1) - x) &= 0; \\ x_1 &= 1; \end{aligned}$$

$$\begin{aligned} x^3 - 6x - 6 - x &= 0; \\ x(x^2 - 1) - 6(x + 1) &= 0; \\ x(x - 1)(x + 1) - 6(x + 1) &= 0; \\ (x + 1)(x(x - 1) - 6) &= 0; \\ x_2 &= -1; \\ x^2 - x - 6 &= 0; \\ x_3 &= 3; \\ x_4 &= -2; \end{aligned}$$

Answer: 1; -1; 3; -2;

$$\begin{aligned} x^3 + 4x^2 - 5 &= 0; \\ x^3 - x^2 + 5x^2 - 5 &= 0; \\ x^2(x - 1) + 5(x^2 - 1) &= 0; \\ x^2(x - 1) + 5(x - 1)(x + 1) &= 0; \\ (x - 1)(x^2 + 5(x + 1)) &= 0; \\ x_1 &= 1; \\ x^2 + 5x + 5 &= 0 \\ D = 25 - 20 &= 5; D > 0; \\ x_2 = (-5 - V5)/2 &= \\ x_3 = (-5 + V5)/2 &= \end{aligned}$$

Answer: 1; (-5 - V5)/2; (-5 + V5)/2;

$$\begin{aligned} x^4 - x^3 - 13x^2 + x + 12 &= 0; \\ x^3(x - 1) - 12x^2 - x^2 + x + 12 &= 0; \\ x^3(x - 1) - 12x^2 + 12 - x^2 + x &= 0; \\ x^3(x - 1) - 12(x^2 - 1) - x(x - 1) &= 0; \\ x^3(x - 1) - 12(x - 1)(x + 1) - x(x - 1) &= 0; \\ (x - 1)(x^3 - 12(x + 1) - x) &= 0; \\ x_1 &= 1; \\ x^3 - 13x - 12 &= 0; \\ x^3 - 12x - x - 12 &= 0 \\ x(x^2 - 1) - 12(x + 1) &= 0; \\ x(x - 1)(x + 1) - 12(x + 1) &= 0; \\ (x + 1)(x(x - 1) - 12) &= 0; \\ x_2 &= -1; \\ x^2 - x - 12 &= 0; \\ D = 1 + 48 &= 49; D > 0; VD = 7; \\ x_3 = 1 - 7/2 &= -3; \\ x_4 = 1 + 7/2 &= 4; \end{aligned}$$

Answer: 1; -1; -3; 4