

Уравнение с параметрами (решить уравнение при всех значениях a)

$$x^4 - 3x^2 + 2(a - 1)x + 2a - a^2 = 0$$

$$-a^2 + 2a + 2ax - 2x - 3x^2 + x^4 = 0$$

$$-a^2 + a(2 + 2x) - 2x - 3x^2 + x^4 = 0$$

$$D1 = (1 + x)^2 - (-1) \cdot (-2x - 3x^2 + x^4) =$$

$$1 + 2x + x^2 - 2x - 3x^2 + x^4 = 1 - 2x^2 + x^4 = (1 - x^2)^2$$

$$a1 = -(1 + x) - (1 - x^2) / -1 = (-1 - x - 1 + x^2) / -1 = -(-x^2 + x + 2)$$

$$a2 = -(1 + x) + (1 - x^2) / -1 = (-1 - x + 1 - x^2) / -1 = 1 + x - 1 + x^2 = x^2 + x$$

$$-(a - [-x^2 + x + 2]) \cdot (a - [x^2 + x]) = 0$$

$$-x^2 + x + 2 = a;$$

$$-x^2 + x + 2 - a = 0$$

$$D = 1 - (-4) \cdot (2 - a) = 1 + 8 - 4a = 9 - 4a$$

$$9 - 4a > 0$$

$$a < 9/4$$

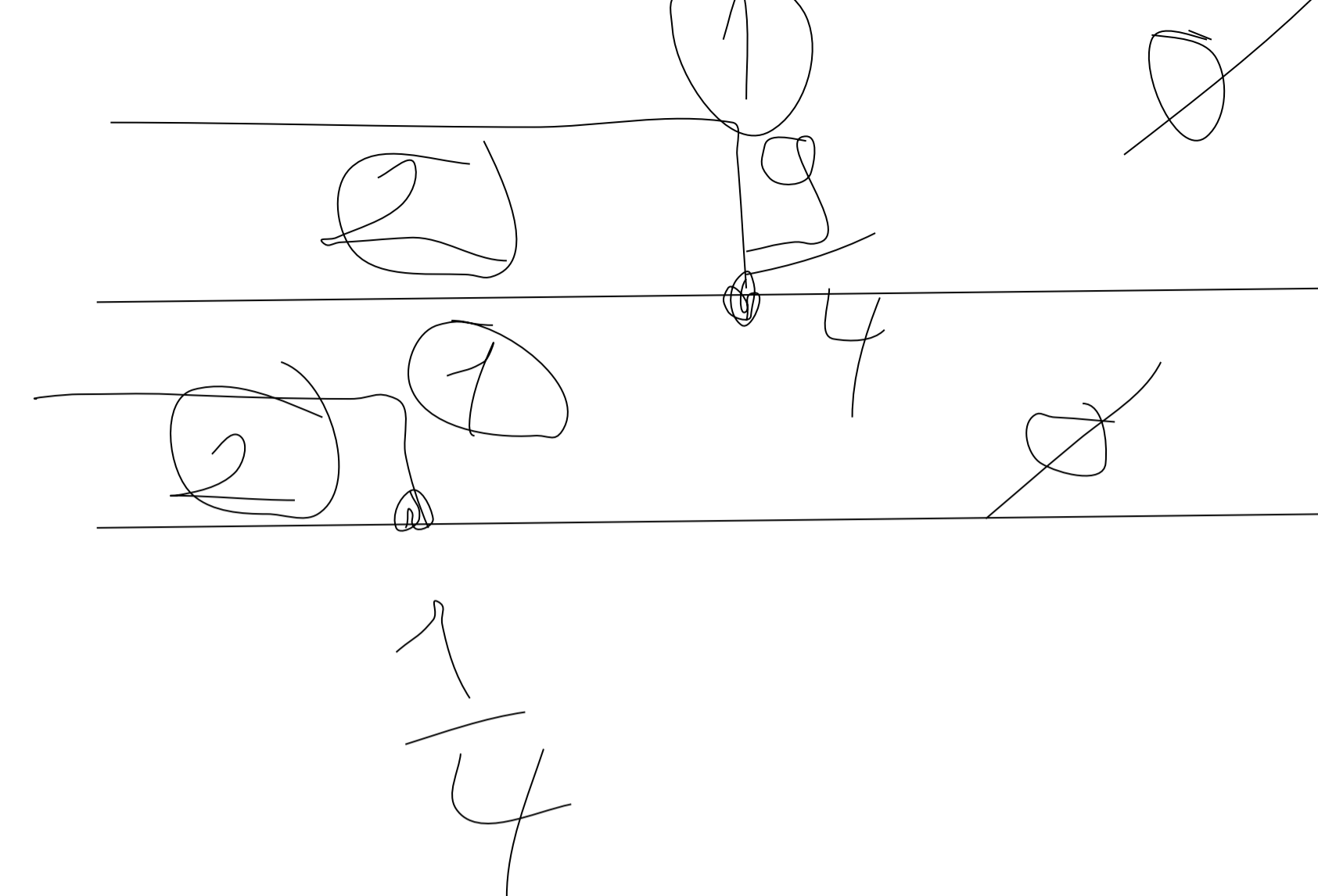
$$x1 = -1 + \sqrt{9 - 4a} / -2 = [1 - \sqrt{9 - 4a}] / 2$$

$$x2 = -1 - \sqrt{9 - 4a} / -2 = [1 + \sqrt{9 - 4a}] / 2$$

$$a = 9/4$$

$$x = -1 / -2 = 1/2$$

$a > 9/4$ корней нет



$$x^2 + x = a$$

$$x^2 + x - a = 0$$

$$D = 1 - 4a$$

$$1 - 4a > 0$$

$$a < 1/4$$

$$x1 = [-1 - \sqrt{1 - 4a}] / 2$$

$$x2 = [-1 + \sqrt{1 - 4a}] / 2$$

$$a = 1/4$$

$$x = -1/2$$

$$a > 1/4$$

корней нет

$a \in (-\infty; 1/4)$ 4 корня

$$x1 = [1 - \sqrt{9 - 4a}] / 2$$

$$x2 = [1 + \sqrt{9 - 4a}] / 2$$

$$x3 = [-1 - \sqrt{1 - 4a}] / 2$$

$$x4 = [-1 + \sqrt{1 - 4a}] / 2$$

$a = 1/4$ 3 корня

$$x1 = [1 - \sqrt{9 - 4a}] / 2$$

$$x2 = [1 + \sqrt{9 - 4a}] / 2$$

$$x3 = -1/2$$

$a \in (1/4; 9/4)$ 2 корня

$$x1 = [1 - \sqrt{9 - 4a}] / 2$$

$$x2 = [1 + \sqrt{9 - 4a}] / 2$$

$a = 9/4$ 1 корень

$$x = 1/2$$

$a > 9/4$ корней нет