

$$|a|=|b| \quad ^2$$

$$a^2=b^2$$

$$a^2-b^2=0$$

$$(a-b)(a+b)=0$$

$$a=b \text{ или } a=-b$$

$$|a|=0$$

1) $|3x^2 - 3x + 5| = |2x^2 + 6x - 3|$
 $(3x^2 - 3x + 5)^2 - (2x^2 + 6x - 3)^2 = 0$
 $(3x^2 - 3x + 5 - 2x^2 - 6x + 3)(3x^2 - 3x + 5 + 2x^2 + 6x - 3) = 0$
 $x^2 - 9x + 8 = 0$
 $x_1 = 8$
 $x_2 = 1$
 $D = 9 - 40 = -31$
 Ответ: 8; 1

И 2 примера из предыдущего документа

2) $|x+5| - |x-3| = 8$
 $|x+5| = 8 + |x-3|$
 $(x+5)^2 = 64 + 16|x-3| + (x-3)^2$
 $(x+5)^2 - (x-3)^2 - 64 = 16|x-3|$
 $(x+5-x+3)(x+5+x-3) - 64 = 16|x-3|$
 $16x + 16 - 64 = 16|x-3|$
 $x + 1 - 4 = |x-3|$
 1) $x - 3 = x - 3$
 2) $x - 3 = 3 - x$

- 1) любое число
- 2) $x = 3$

Ответ: любое число

$$|A| \cdot |B| = |A \cdot B|$$



$$|a| = \begin{cases} a, & a > 0 \\ -a, & a \leq 0 \end{cases}$$

1) $|3x^2 - 3x + 5| = |2x^2 + 6x - 3|$

3) $|x - 1| - 2|x - 2| + 3|x - 3| = 4$

4) $x^2 - 5x - 6|x|/x = 0$

5) $x^2 - 4x|x - \pi|/(x - \pi) + 2 = 0$

$$2x - x = 5 - 1$$

$$x = 4$$

$$2x - x = 5 - 1 \quad |^2$$

$$4x^2 - 4x^2 + x^2 = 16$$

$$x^2 = 16$$

$$x = \pm 4$$

$$|2x - x| = 5 - 1$$

$$|x| = 4$$

$$x = 4$$

$$x = -4$$

$$|2x - x| = 5 - 1 \quad |^2$$

$$|2x - x|^2 = 16$$

$$|x|^2 = 16$$

$$x^2 = 16$$

$$x = \pm 4$$

$$|x - 1| - 2|x - 2| + 3|x - 3| = 4$$

$$|x - 1| + 3|x - 3| = 4 + 2|x - 2|$$

$$|x - 1|^2 + 6|x - 1| \cdot |x - 3| + 9|x - 3|^2 = 16 + 16|x - 2| + 4|x - 2|^2$$

$$(x - 1)^2 + 6|x - 1| \cdot |x - 3| + 9(x - 3)^2 = 16 + 16|x - 2| + 4(x - 2)^2$$

$$x^2 - 2x + 1 + 6|x - 1| \cdot |x - 3| + 9x^2 - 54x + 81 = 16 + 16|x - 2| + 4x^2 - 16x + 16$$

$$10x^2 - 56x + 82 + 6|x - 1| \cdot |x - 3| = 4x^2 - 16x + 32 + 16|x - 2|$$

$$6x^2 - 30x + 50 + 6|x - 1| \cdot |x - 3| - 16|x - 2| = 0$$

$$3x^2 - 15x + 25 + 3|x - 1| \cdot |x - 3| - 8|x - 2| = 0$$

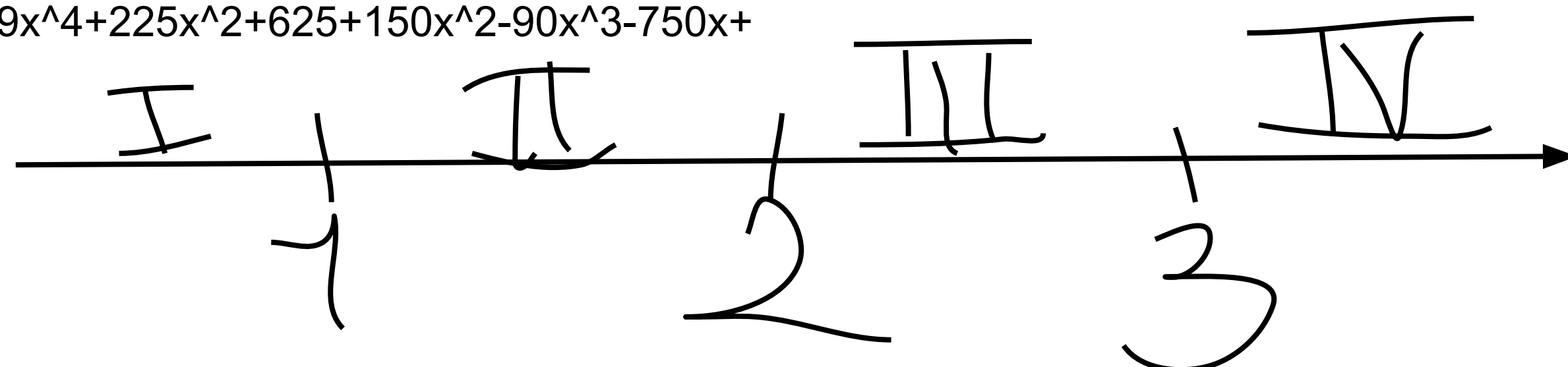
$$D = 225 - 300 = -75$$

$$f(x) = 3x^2 - 15x + 25 \quad D < 0$$

$$3x^2 - 15x + 25 + 3|x - 1| \cdot |x - 3| = 8|x - 2|$$

$$9x^4 + 225x^2 + 625 + 150x^2 - 90x^3 - 750x + 2(3x^2 - 15x + 25)(3|x - 1| \cdot |x - 3|) + 9(x - 1)^2 \cdot (x - 3)^2 = 64(x - 2)^2$$

$$9x^4 + 225x^2 + 625 + 150x^2 - 90x^3 - 750x +$$



I) $x < 1$

$$-(x - 1) + 2(x - 2) - 3(x - 3) = 4$$

$$1 - x + 2x - 4 - 3x + 9 = 4$$

$$2 - 2x = 0$$

$$2x - 2 = 0$$

$$x = 1$$

II) $1 \leq x < 2$

$$x - 1 + 2(x - 2) - 3(x - 3) = 4$$

$$x - 1 + 2x - 4 - 3x + 9 = 4$$

$$3x - 3x = 0$$

$$x \in [1; 2]$$

III) $2 < x < 3$

$$x - 1 - 2(x - 2) - 3(x - 3) = 4$$

$$x - 1 - 2x + 4 - 3x + 9 = 4$$

$$-4x + 12 = 4$$

$$4x = 8$$

$$x = 2$$

IV) $3 < x$

$$(x - 1) - 2(x - 2) + 3(x - 3) = 4$$

$$x - 1 - 2x + 4 + 3x - 9 = 4$$

$$2x - 10 = 0$$

$$2x = 10$$

$$x = 5$$

Ответ: $x \in [1; 2] \cup \{5\}$

4) $x^2 - 5x - 6|x|/x = 0$

$$x \neq 0$$

I) $x > 0$

$$x^2 - 5x - 6x/x = 0$$

$$x^2 - 5x - 6 = 0$$

$$x_1 = 6$$

$$x_2 = -1$$

II) $x < 0$

$$x^2 - 5x + 6x/x = 0$$

$$x^2 - 5x + 6 = 0$$

$$x_1 = 2$$

$$x_2 = 3$$

Ответ: 6

5) $x^2 - 4x|x - \pi|/(x - \pi) + 2 = 0$

$$x \neq \pi$$

I) $x > \pi$

$$x^2 - 4x(x - \pi)/(x - \pi) + 2 = 0$$

$$x^2 - 4x + 2 = 0$$

$$D = 4 - 2 = 2$$

$$x_1 = (2 - \sqrt{2})$$

$$x_2 = (2 + \sqrt{2})$$

$$3,141592653589793238462643$$

II) $x < \pi$

$$x^2 + 4x(x - \pi)/(x - \pi) + 2 = 0$$

$$x^2 + 4x + 2 = 0$$

$$x_3 = (-2 - \sqrt{2})$$

$$x_4 = (-2 + \sqrt{2})$$

Ответ: $(2 + \sqrt{2}); (-2 - \sqrt{2}); (-2 + \sqrt{2})$