

$$\cos x + \cos 2x + \dots + \cos(n-1)x + \cos nx = \frac{\sin(nx/2) \cos(x(n+1)/2)}{\sin(x/2)}$$

$$\cos(2P/7) + \cos(2 \cdot 2P/7) + \cos(3 \cdot 2P/7) = \frac{\sin(3P/7) \cos(4P/7)}{\sin(P/7)} = \frac{(0 - \sin(P/7))}{(2 \sin P/7)} = -\frac{1}{2}$$

$$\cos(2P/7) \cdot \cos(2 \cdot 2P/7) \cdot \cos(3 \cdot 2P/7) = \cos x \cdot \cos 2x \cdot \cos 3x = \frac{1}{2} (\cos 4x + \cos 2x) \cos 2x = \frac{1}{2} (\cos 4x \cos 2x + \cos^2(2x))$$

$$A = \cos x \cdot \cos 2x \cdot \cos 3x$$

$$A \sin x = \cos x \cdot \sin x \cdot \cos 2x \cdot \cos 3x$$

$$A \sin x = \frac{1}{2} \sin 2x \cdot \cos 2x \cdot \cos 3x$$

$$A \sin x = \frac{1}{4} (\sin 4x \cdot \cos 3x) = \frac{1}{8} (\sin 7x + \sin x)$$

$$A = \frac{1}{8} (\sin 7x + \sin x) / \sin x$$

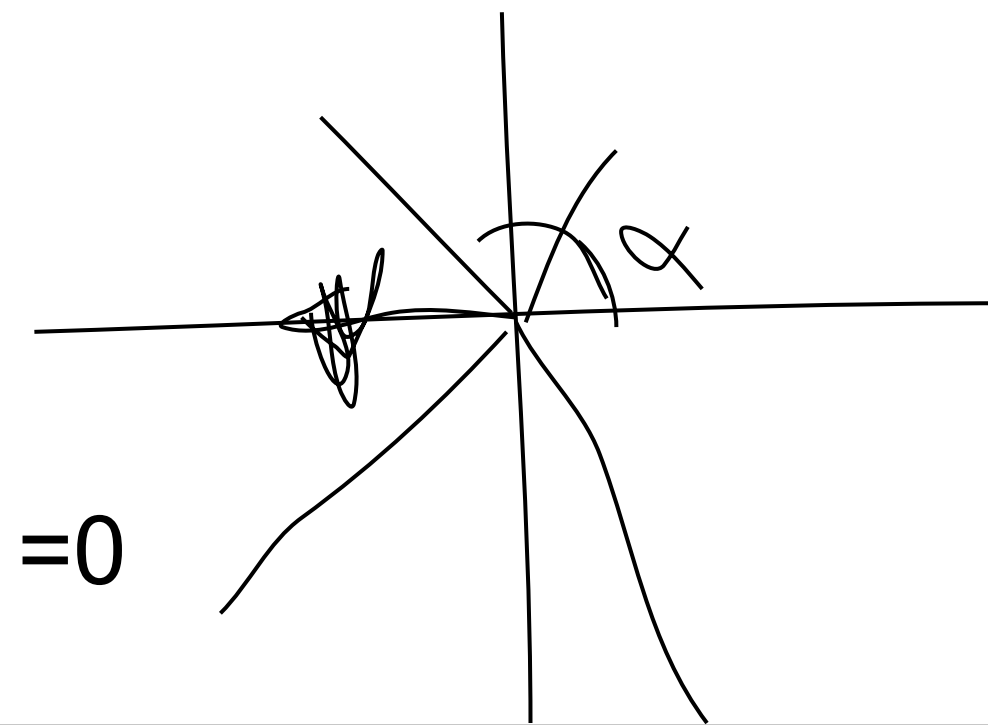
$$A = \frac{1}{8} (\sin(2P) / \sin x + 1) = \frac{1}{8}$$

7.32

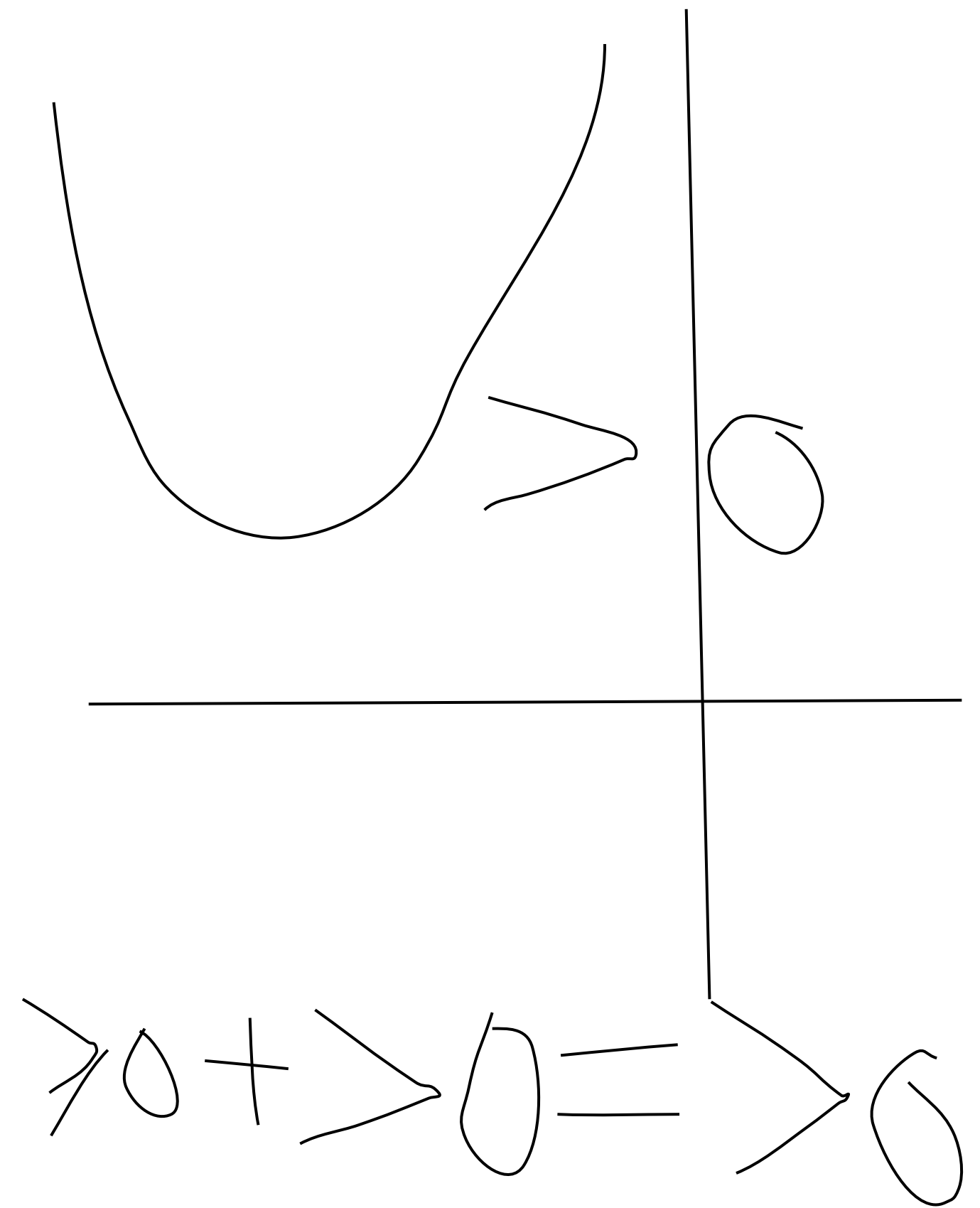
$$x^4 + x^3 + x^2 + x + 1 = 0$$

$$x = |z|(\cos a + i \sin a)$$

$$|z|^4(\cos 4a + i \sin 4a) + |z|^3(\cos 3a + i \sin 3a) + |z|^2(\cos 2a + i \sin 2a) + |z|(\cos a + i \sin a) + 1 = 0$$



7.32-7.35



$$z^4 + z^3 + z^2 + z + 1 = 0$$

$$z^2 + z + 1 + 1/z + 1/z^2 = 0$$

$$z^2 + 1/z^2 + z + 1/z + 1 = 0$$

$$z + 1/z = w$$

$$w^2 = z^2 + 2z/z + 1/z^2 \Rightarrow z^2 + 1/z^2 = w^2 - 2$$

$$(w)^2 + (w) - 1 = 0$$

$$w^2 + w - 1 = 0$$

$$D = 1 + 4 = 5$$

$$w = \frac{-1 \pm \sqrt{5}}{2}$$

$$z + 1/z = \frac{-1 + \sqrt{5}}{2}$$

$$z^2 + (1 + \sqrt{5})/2 \cdot z + 1 = 0$$

$$z^2 + (1 + \sqrt{5})/2 \cdot z + 1 = 0$$

$$D = 3/2 + \sqrt{5}/2 - 4 = \sqrt{5}/2 - 5/2$$

$$z = \frac{-1 - \sqrt{5} \pm \sqrt{\sqrt{5}/2 - 5/2}}{2}$$

$$z^2 + (1 - \sqrt{5})/2 \cdot z + 1 = 0$$

$$D = 3/2 - \sqrt{5}/2 - 4 = -\sqrt{5}/2 - 5/2$$

$$z = \frac{-1 - \sqrt{5} \pm \sqrt{-\sqrt{5}/2 - 5/2}}{2}$$