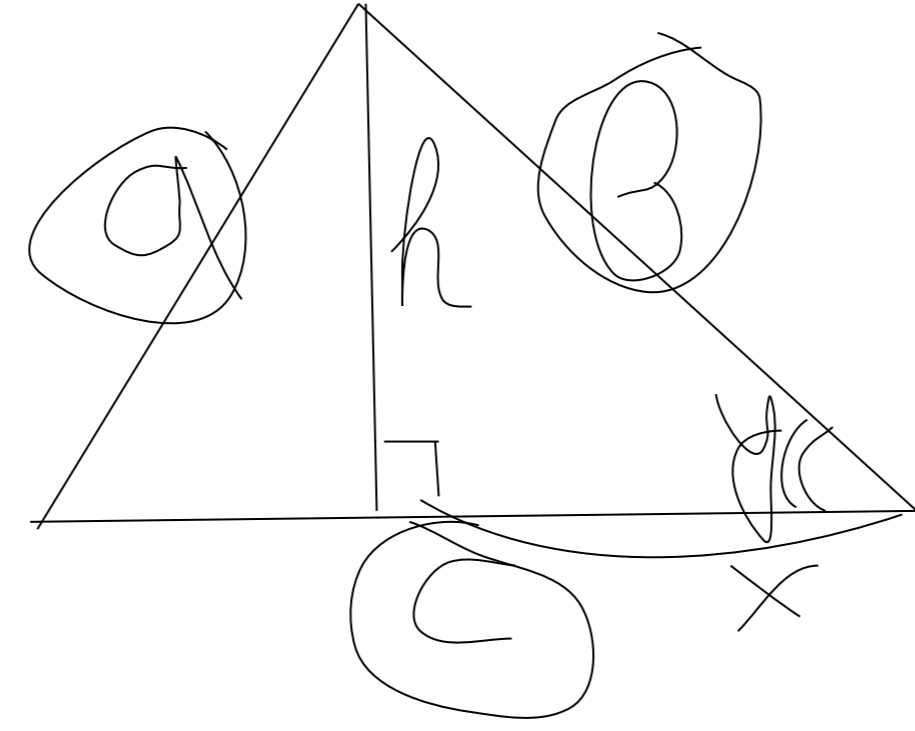


Дан треугольник ABC, и три его стороны a,b,c. найти h



$$a^2 = b^2 + c^2 - 2bc \cos Y$$

$$2bc \cos Y = b^2 + c^2 - a^2$$

$$\cos Y = (b^2 + c^2 - a^2) / 2bc$$

$$h^2 = b^2 - x^2$$

$$x = \cos Y \cdot b$$

$$h^2 = b^2 - \cos^2 Y \cdot b^2$$

$$h^2 = b^2 - (b^2 + c^2 - a^2)^2 / (4b^2c^2)$$

$$h^2 = b^2 - (b^2 + c^2 - a^2)^2 / (4c^2) = 4b^2c^2 - (b^2 + c^2 - a^2)^2 / (4c^2)$$

$$h^2 = (2bc - b^2 - c^2 + a^2)(2bc + b^2 + c^2 - a^2) / (4c^2)$$

$$h^2(4c^2) = (2bc - b^2 - c^2 + a^2)(2bc + b^2 + c^2 - a^2)$$

$$h^2(4c^2) = -(-2bc + b^2 + c^2 - a^2)(2bc + b^2 + c^2 - a^2)$$

$$h^2(4c^2) = -((b-c)^2 - a^2)(2bc + b^2 + c^2 - a^2) = (-b+c+a)(b-c+a)((b+c)^2 - a^2)$$

$$h^2(4c^2) = (-b+c+a)(b-c+a)(b+c-a)(b+c+a)$$

$$h^2(4c^2) = (-b+c+a+b-b)(b-c+a+c-c)(b+c-a+a-a)(b+c+a)$$

$$h^2(4c^2) = (2p-2b)(2p-2c)(2p-2a)(2p)$$

$$h^2(4c^2) = 2^4(p-b)(p-c)(p-a)(p)$$

$$2hc = 4V\{(p-b)(p-c)(p-a)(p)\}$$

$$hc = 2V\{(p-b)(p-c)(p-a)(p)\}$$

следствие 1

$$h = 2V\{(p-b)(p-c)(p-a)(p)\} / c$$

$$(x-y)^2 = (y-x)^2$$

$$(a+b+c)/2 = p$$

$$2p = (a+b+c)$$

$$-2bc + b^2 + c^2 = (b-c)^2$$

$$f(b,c) = -2bc + b^2 + c^2 = b^2(-2c/b + 1 + c^2/b^2)$$

$$c/b = k$$

$$= b^2(-2k + 1 + k^2) = b^2(k-1)^2$$

$$-2k + 1 + k^2 = 0$$

$$k_1 = 1$$

$$k_2 = 1$$

$$-2k + 1 + k^2 = 1 \cdot (k-k_1)(k-k_2) = (k-1)(k-1) = (k-1)^2$$

$$= b^2(k-1)^2 = b^2(c/b-1)^2 = b^2(c/b-1)^2 = b^2(c-b)^2/b^2 = (c-b)^2$$

следствие 2 формула Герона

$$S = hc/2 = V\{(p-b)(p-c)(p-a)(p)\}$$