

$$2. a_n = 1 + \frac{1}{10} + \frac{1}{100} + \frac{1}{1000} + \dots + \frac{1}{10^{n-1}}. \text{ Найти } \lim a_n$$

$$a_n = 1 + 1/10 + 1/100 + 1/1000 + \dots + 1/10^{(n-1)}$$

$$1,1111\dots = 1/(1-1/10) = 10/9$$

$$(10^{(n-1)} + 10^{(n-2)} + \dots + 1)/10^{(n-1)}$$

$$S_n = b_1 + b_1 \cdot q + b_1 \cdot q^2 + \dots + b_1 q^{(n-2)} + b_1 \cdot q^{(n-1)}$$

$$b_1 + b_1 \cdot q + b_1 \cdot q^2 + \dots + b_1 q^{(n-2)} = S_n - b_1 \cdot q^{(n-1)}$$

$$S_n = b_1 + b_1 \cdot q + b_1 \cdot q^2 + \dots + b_1 q^{(n-2)} + b_1 \cdot q^{(n-1)} = b_1 + q(b_1 + b_1 q + \dots + b_1 q^{(n-2)}) = b_1 + q(S_n - b_1 \cdot q^{(n-1)})$$

$$S_n = b_1 + q(S_n - b_1 \cdot q^{(n-1)})$$

$$S_n - q S_n = b_1 - b_1 \cdot q^n$$

$$S_n = b_1(1 - q^n)/(1 - q)$$

$$S_{\infty} = \lim_{n \rightarrow \infty} (b_1(1 - q^n)/(1 - q)) = b_1/(1 - q)$$