

$$\sin^8 x + \cos^8 x = 17/16 \cos^2 2x$$

$$(\sin^2 x)^4 + (\cos^2 x)^4 = 17/16 \cos^2 2x$$

$$((1-\cos 2x)/2)^4 + ((\cos 2x+1)/2)^4 = 17/16 \cos^2 2x$$

$$\cos 2x = t$$

$$((1-t)/2)^4 + ((t+1)/2)^4 = 17/16 t^2$$

$$(1-t)^4/16 + (t+1)^4/16 = 17/16 t^2$$

$$17/16 t^2 - (1-t)^4/16 - (t+1)^4/16 = 0$$

$$(17t^2 - (1-t)^4 - (t+1)^4)/16 = 0$$

$$17t^2 - t^4 + 4t^3 - 6t^2 + 4t - 1 - t^4 - 4t^3 - 6t^2 - 4t - 1 = 0$$

$$-2t^2 - 5t^2 - 2 = 0$$

$$17t^2 - (1-t)^4 - (t+1)^4 = 0$$

$$t^2 = x$$

$$-2x^2 + 5x - 2 = 0$$

$$2x^2 - 5x + 2 = 0$$

$$D = 9$$

$$x_1 = (5-3)/4 = 1/2$$

$$x_2 = (5+3)/4 = 2$$

$$t^2 = 1/2$$

$$t = \pm 1/\sqrt{2}$$

$$t^2 = 2$$

$$t = \pm \sqrt{2}$$

$$\cos 2x = 1/\sqrt{2}$$

$$2x = \pm \pi/4 + 2\pi n$$

$$x = \pm \pi/8 + \pi n$$

$$\cos 2x = -1/\sqrt{2}$$

$$2x = \pm 3\pi/4 + 2\pi n$$

$$x = \pm 3\pi/8 + \pi n$$

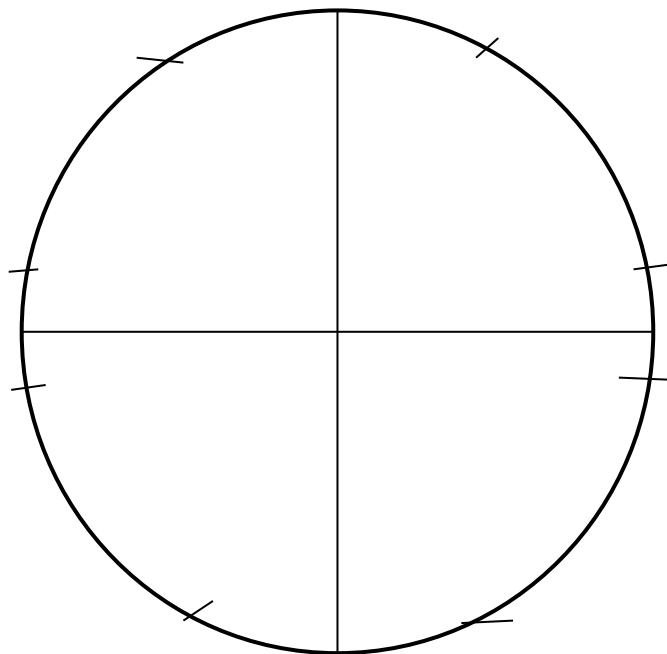
$$\cos 2x = \sqrt{2}$$

$$\text{Нет}$$

$$\cos 2x = -\sqrt{2}$$

$$\text{Нет}$$

Ответ1: $\pm \pi/8 + \pi n$; $\pm 3\pi/8 + \pi n$.
 Ответ2: $\pi/8 + \pi n/4$.



$$\sin^2 x = (1 - \cos 2x)/2$$

$$\cos^2 x = (\cos 2x + 1)/2$$

$$t^4 - 4t^3 + 6t^2 - 4t + 1$$

$$\begin{array}{cccc} & & 1 & & 1 & & & & \\ & & & 1 & & 2 & & 1 & & \\ & & & & 1 & & 3 & & 3 & & 1 \\ & & & & & 1 & & 4 & & 6 & & 4 & & 1 \end{array}$$