

$$2\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x$$

$$\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x - \operatorname{tg}x$$

$$\sin x / \cos x + \sin 2x / \cos 2x = \sin 4x / \cos 4x - \sin x / \cos x$$

$$(\sin x \cdot \cos 2x + \sin 2x \cdot \cos x) / (\cos x \cdot \cos 2x) = (\sin 4x \cdot \cos x - \sin x \cdot \cos 4x) / (\cos x \cdot \cos 4x)$$

$$\sin(x+2x) / (\cos x \cdot \cos 2x) = \sin(4x-x) / (\cos x \cdot \cos 4x)$$

$$\sin(3x) / (\cos x \cdot \cos 2x) - \sin(3x) / (\cos x \cdot \cos 4x) = 0$$

$$\sin 3x (1 / (\cos x \cdot \cos 2x) - 1 / (\cos x \cdot \cos 4x)) = 0$$

$$\sin 3x = 0$$

$$3x = \pi k$$

$$x = \pi k / 3$$

$$1 / (\cos x \cdot \cos 2x) - 1 / (\cos x \cdot \cos 4x) = 0$$

$$(\cos 4x - \cos 2x) / (\cos x \cdot \cos 2x \cdot \cos 4x) = 0$$

$$(\cos x \cdot \cos 2x \cdot \cos 4x) \neq 0$$

$$(\cos 4x - \cos 2x) = 0$$

$$2\cos^2 2x - 1 - \cos 2x = 0$$

$$\cos 2x = t$$

$$2t^2 - t - 1 = 0$$

$$D = 1 + 8 = 9$$

$$x_1 = (1 - 3) / 4 = -1/2$$

$$x_2 = (1 + 3) / 4 = 1$$

$$\cos 2x = -1/2$$

$$2x = \pm 2\pi/3 + 2\pi k$$

$$x = \pm \pi/3 + \pi k$$

$$\cos 2x = 1$$

$$2x = 2\pi k$$

$$x = \pi k$$

$$\cos x \neq 0$$

$$x = \pi/3$$

$$x \neq \pi/2 + \pi k$$

$$\cos 2x \neq 0$$

$$2x \neq \pi/2 + \pi k$$

$$x \neq \pi/4 + \pi k/2$$

$$\cos 4x \neq 0$$

$$x \neq \pi/8 + \pi k/4$$

