

$$2\sqrt{3}\sin 5x - \sqrt{3}\sin x = \cos 24x \cdot \cos x + 2\cos 5x - 6$$

$$2\sqrt{3}\sin 5x - 2\cos 5x = \cos 24x \cdot \cos x + \sqrt{3}\sin x - 6$$

$$2\sqrt{3}\sin 5x - 2\cos 5x = \sqrt{(12 + 4)[\sin 5x \cdot \frac{\sqrt{3}}{4} - \cos 5x \cdot \frac{2}{4}]} = \sqrt{(12 + 4)[\sin 5x \cdot \cos \frac{P}{6} - \cos 5x \cdot \sin \frac{P}{6}]} = 4\sin(5x - \frac{P}{6})$$

$$\cos t = \frac{\sqrt{3}}{2}$$

$$\sin t = \frac{1}{2}$$

$$t = \frac{P}{6}$$

$$\cos 24x \cdot \cos x + \sqrt{3}\sin x = \sqrt{(\cos^2(24x) + 3)[\cos x \cdot \frac{\cos 24x}{\sqrt{\cos^2(24x) + 3}} + \sin x \cdot \frac{\sqrt{3}}{\sqrt{\cos^2(24x) + 3}}]} =$$

$$\sqrt{(\cos^2(24x) + 3)[\cos x \cdot \sin t + \sin x \cdot \cos t]} = \sqrt{(\cos^2(24x) + 3)\sin(x+t)}$$

$$\sin t = \frac{\cos 24x}{\sqrt{\cos^2(24x) + 3}}$$

$$\cos t = \frac{\sqrt{3}}{\sqrt{\cos^2(24x) + 3}}$$

$$-2 \leq \sqrt{(\cos^2(24x) + 3)\sin(x+t)} \leq 2$$

$$-4 \leq 4\sin(5x - \frac{P}{6}) \leq 4$$

$$-8 \leq \cos 24x \cdot \cos x + \sqrt{3}\sin x - 6 \leq -4$$

$$\frac{P}{3} + 2\frac{P}{5} =$$

$$= \frac{(5P + 6P)}{15} = \frac{11P}{15}$$

$$\frac{11P}{15} + 2\frac{P}{5} = \frac{17P}{15}$$

$$\frac{17P}{15} + 2\frac{P}{5} = \frac{23P}{15}$$

$$\frac{23P}{15} + 2\frac{P}{5} = \frac{29P}{15}$$

$$\frac{29P}{15} + 2\frac{P}{5} = \frac{35P}{15} = \frac{7P}{3} = 2P + \frac{P}{3}$$

$$4\sin(5x - \frac{P}{6}) = -4$$

$$\sin(5x - \frac{P}{6}) = -1$$

$$5x - \frac{P}{6} = \frac{3P}{2} + 2Pk$$

$$5x = \frac{3P}{2} + 2Pk + \frac{P}{6}$$

$$5x = \frac{10P}{6} + 2Pk$$

$$x = \frac{10P}{30} + \frac{2Pk}{5}$$

$$x = \frac{P}{3} + \frac{2Pk}{5}$$

Четвертая серия проверки

$$x = \frac{29P}{15}$$

$$\cos 24x = \cos 24(\frac{29P}{15}) = \cos(\frac{232P}{5}) = \cos(\frac{230P + 2P}{5}) = \cos(\frac{2P}{5}) \neq 1$$

$$\sqrt{(\cos^2(24x) + 3)\sin(x+t)} - 6 \neq -4$$

Ответ: $x = \frac{P}{3} + 2Pk$

Первая серия проверки

$$x = \frac{P}{3} + 2Pk$$

$$\cos 24x \cdot \cos x + \sqrt{3}\sin x - 6 = \cos 24(\frac{P}{3} + 2Pk) \cdot \cos(\frac{P}{3} + 2Pk) + \sqrt{3}\sin(\frac{P}{3} + 2Pk) - 6 =$$

$$= \cos(8P + 48Pk) \cdot \cos(\frac{P}{3} + 2Pk) + \sqrt{3}\sin(\frac{P}{3} + 2Pk) - 6 = 1 \cdot \frac{1}{2} + \sqrt{3} \cdot \frac{\sqrt{3}}{2} - 6 = \frac{1}{2} + \frac{3}{2} - 6 = -4$$

Вторая серия проверки

$$x = \frac{11P}{15} + 2Pk$$

$$\cos 24x = \cos 24(\frac{11P}{15} + 2Pk) = \cos(\frac{264P}{15} + 48Pk) = \cos(\frac{264P}{15}) = \cos(\frac{(240P + 24P)}{15}) = \cos(\frac{8P}{5}) \neq 1$$

$$\sqrt{(\cos^2(24x) + 3)\sin(x+t)} - 6 \neq -4$$

Третья серия проверки

$$x = \frac{17P}{15}$$

$$\cos 24x = \cos 24(\frac{17P}{15}) = \cos 24(\frac{17P}{15}) = \cos \frac{136P}{5} = \cos(\frac{130P + 6P}{5}) = \cos(\frac{6P}{5}) \neq 1$$

$$\sqrt{(\cos^2(24x) + 3)\sin(x+t)} - 6 \neq -4$$

Четвертая серия проверки

$$x = \frac{23P}{15}$$

$$\cos 24x = \cos 24(\frac{23P}{15}) = \cos(\frac{184P}{5}) = \cos(\frac{180P + 4P}{5}) = \cos(\frac{4P}{5}) \neq 1$$

