

$$3\cos x + 4\sin x = 5\sin 3x$$

найти решения на промежутке $[0; \pi/2]$

$$3\cos x + 4\sin x = 5(3\sin x - 4\sin^3 x)$$

$$3\cos x + 4\sin x = 15\sin x - 20\sin^3 x$$

$$3\cos x + 20\sin^3 x = 15\sin x - 4\sin x$$

$$4\cos x + 20\sin^3 x = 11\sin x$$

$$5(3\cos x/5 + 4\sin x/5) = 5\sin 3x$$

$$5(\cos x \cdot \sin a + \sin x \cdot \cos a) = 5\sin 3x$$

$$\sin a = \frac{3}{5}$$

$$a = \arcsin\left(\frac{3}{5}\right)$$

$$\cos a = \frac{4}{5}$$

$$a = \arccos\left(\frac{4}{5}\right)$$

$$5\cos x \sin(\arcsin(\frac{3}{5})) + 5\sin x \cos(\arcsin(\frac{3}{5})) = 5\sin 3x$$

$$\cos x \sin(\arcsin(\frac{3}{5})) + \sin x \cos(\arcsin(\frac{3}{5})) = \sin 3x$$

$$\sin(x + \arcsin(\frac{3}{5})) = \sin 3x$$

$$\sin(x + \arcsin(\frac{3}{5})) - \sin 3x = 0$$

$$2\cos\left(\frac{4x + \arcsin(\frac{3}{5})}{2}\right) \cdot \sin\left(\frac{\arcsin(\frac{3}{5}) - 2x}{2}\right) = 0$$

$$2\cos\left(\frac{4x + \arcsin(\frac{3}{5})}{2}\right) = 0$$

$$\frac{4x + \arcsin(\frac{3}{5})}{2} = \frac{\pi}{2} + \pi k$$

$$4x + \arcsin(\frac{3}{5}) = \pi + 2\pi k$$

$$4x = 2\pi k - \arcsin(\frac{3}{5}) + \pi$$

$$x = \frac{\pi k}{2} - \frac{\arcsin(\frac{3}{5})}{4} + \frac{\pi}{4}$$

$$x_2 = -\frac{\arcsin(\frac{3}{5})}{4} + \frac{\pi}{4}$$

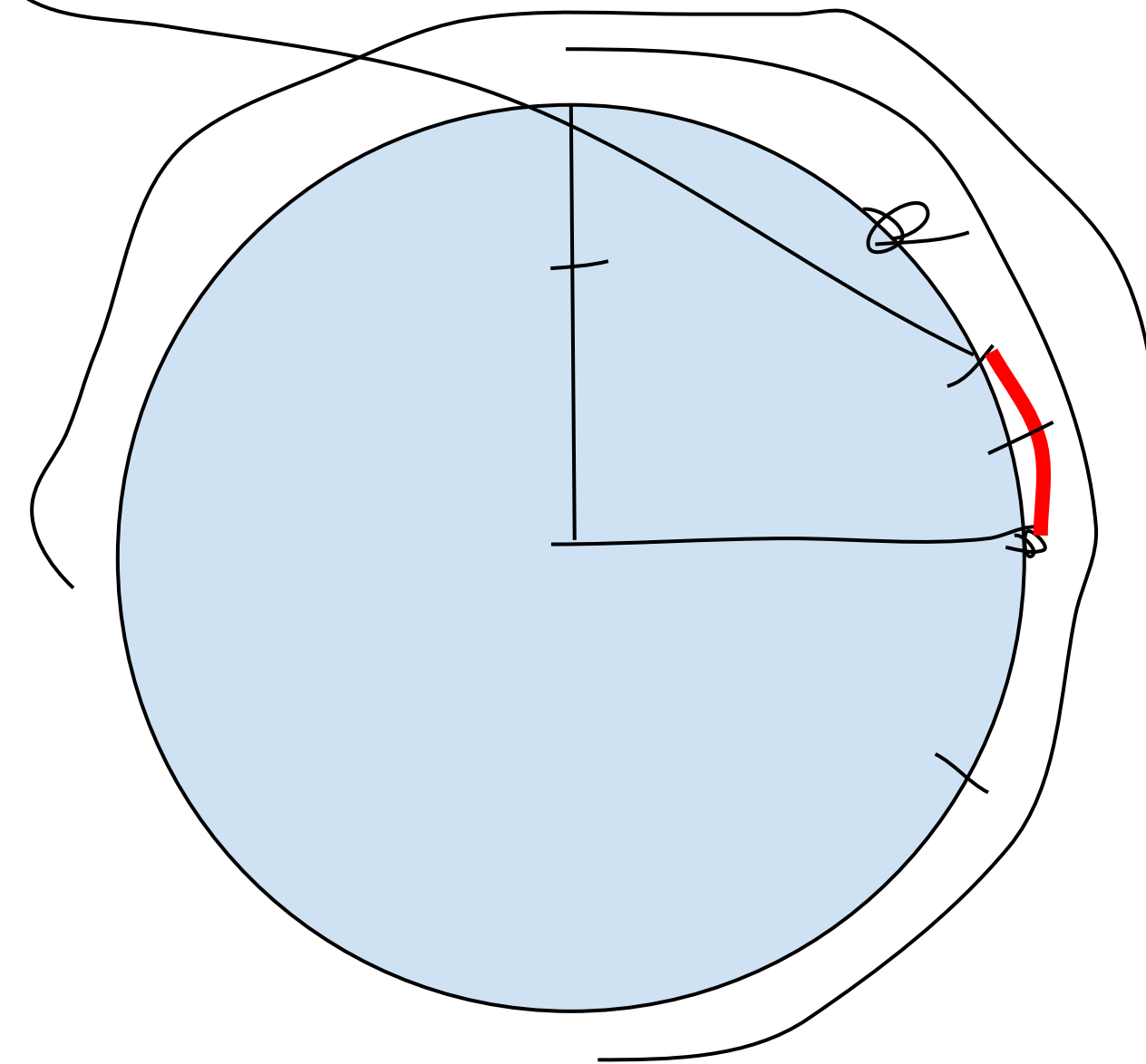
$$\sin\left(\frac{\arcsin(\frac{3}{5}) - 2x}{2}\right) = 0$$

$$\frac{\arcsin(\frac{3}{5}) - 2x}{2} = \pi k$$

$$\arcsin(\frac{3}{5}) - 2x = 2\pi k$$

$$x = \frac{\arcsin(\frac{3}{5})}{2} - \pi k$$

$$x_1 = \frac{\arcsin(\frac{3}{5})}{2}$$



Ответ: $\frac{\arcsin(\frac{3}{5})}{2}$
 $-\frac{\arcsin(\frac{3}{5})}{4} + \frac{\pi}{4}$