

$$1/(\operatorname{tg}5x + \operatorname{tg}2x) - 1/(\operatorname{ctg}5x + \operatorname{ctg}2x) = \operatorname{tg}3x$$

$$1/(\sin5x/\cos5x + \sin2x/\cos2x) - 1/(\cos5x/\sin5x + \cos2x/\sin2x) = \sin3x/\cos3x$$

$$1/([\sin5x \cdot \cos2x + \sin2x \cdot \cos5x]/\cos5x \cdot \cos2x) - 1/([\cos5x \cdot \sin2x + \cos2x \cdot \sin5x]/\sin2x \cdot \sin5x) = \sin3x/\cos3x$$

$$\cos5x \cdot \cos2x / [\sin5x \cdot \cos2x + \sin2x \cdot \cos5x] - \sin2x \cdot \sin5x / [\cos5x \cdot \sin2x + \cos2x \cdot \sin5x] = \sin3x/\cos3x$$

$$\cos5x \cdot \cos2x / \sin(5x+2x) - \sin2x \cdot \sin5x / \sin(5x+2x) = \sin3x/\cos3x$$

$$[\cos5x \cdot \cos2x - \sin2x \cdot \sin5x] / \sin(5x+2x) = \sin3x/\cos3x$$

$$\cos(5x+2x) / \sin(5x+2x) = \sin3x/\cos3x$$

$$\cos7x / \sin7x = \sin3x/\cos3x$$

$$\cos7x / \sin7x - \sin3x/\cos3x = 0$$

$$[\cos7x \cdot \cos3x - \sin3x \cdot \sin7x] / \cos3x \cdot \sin7x = 0$$

$$[\cos7x \cdot \cos3x - \sin3x \cdot \sin7x] / \cos3x \cdot \sin7x = 0$$

$$[\cos7x \cdot \cos3x - \sin3x \cdot \sin7x] = 0$$

$$\cos7x \cdot \cos3x - \sin3x \cdot \sin7x = 0$$

$$\cos(7x+3x) = 0$$

$$\cos10x = 0$$

$$10x = P/2 + Pn$$

$$x = P/20 + Pn/10$$

$$\begin{aligned} ax+by &= c \\ x &= x_0 - bt \\ y &= y_0 + at \end{aligned}$$

$$\begin{aligned} x &= x_0 + bt \\ y &= y_0 - at \end{aligned}$$

$$P/20 + Pn/10 \neq Pk/2 \mid (20/P)$$

$$1 + 2n \neq 10k$$

$$1 \neq 10k - 2n \text{ нет решения}$$

$$P/20 + Pn/10 \neq P/4 + Pk/2 \mid (20/P)$$

$$1 + 2n \neq 5 + 10k$$

$$-4 \neq 10k - 2n$$

$$-2 \neq 5k - n$$

$$k_0 = 1 \quad n_0 = 7$$

$$-2 \neq 5k_0 - n_0$$

$$-2 \neq 5(k_0 + a \cdot t) - (n_0 + b \cdot t) =$$

$$= 5k_0 + 5a \cdot t - n_0 - b \cdot t = 5k_0 - n_0 + 5a \cdot t - b \cdot t$$

$$a = 1 \quad b = 5$$

$$k = k_0 + 1 \cdot t = 1 + t$$

$$n = n_0 + 5t = 7 + 5t$$

$$\sin2x \neq 0$$

$$x \neq Pk/2$$

$$\cos2x \neq 0$$

$$x \neq P/4 + Pk/2$$

$$\cos3x \neq 0$$

$$x \neq P/6 + Pk/3$$

$$\cos5x \neq 0$$

$$x \neq P/10 + Pk/5$$

$$\sin5x \neq 0$$

$$x \neq Pk/5$$

$$\sin7x \neq 0$$

$$x \neq Pk/7$$

$$P/20 + Pn/10 \neq P/6 + Pk/3$$

$$1/20 + n/10 \neq [1+2k]/6$$

$$1/20 + n/10 \neq [1+2k]/6 \mid \cdot 60$$

$$3 + 6n \neq 10[1+2k]$$

$$3 + 6n \neq 10 + 20k$$

$$20k - 6n \neq -7 \text{ реш нет}$$

$$P/20 + Pn/10 \neq P/10 + Pk/5$$

$$1 + 2n \neq 2 + 4k$$

$$2n - 4k \neq 1 \text{ реш нет}$$

$$P/20 + Pn/10 \neq Pk/5$$

$$1 + 2n \neq 4k \text{ реш нет}$$

$$P/20 + Pn/10 \neq Pk/7$$

$$7 + 14n \neq 20k$$

$$7 \neq 20k - 14n \text{ реш нет}$$

Ответ $P/20 + Pn/10$, где n целое и $n \neq 7 + 5t$, где t произвольное целое