

$$1/(\operatorname{tg}5x + \operatorname{tg}2x) - 1/(\operatorname{ctg}5x + \operatorname{ctg}2x) = \operatorname{tg}3x$$

$$1/(\sin5x/\cos5x + \sin2x/\cos2x) - 1/(\cos5x/\sin5x + \cos2x/\sin2x) = \sin3x/\cos3x$$

$$1/(\sin5x \cdot \cos2x + \sin2x \cdot \cos5x)/\cos5x \cdot \cos2x - 1/(\cos5x \cdot \sin2x + \cos2x \cdot \sin5x)/\sin2x \cdot \sin5x = \sin3x/\cos3x$$

$$\cos5x \cdot \cos2x / (\sin5x \cdot \cos2x + \sin2x \cdot \cos5x) - \sin2x \cdot \sin5x / (\cos5x \cdot \sin2x + \cos2x \cdot \sin5x) = \sin3x/\cos3x$$

$$\cos5x \cdot \cos2x / \sin(5x+2x) - \sin2x \cdot \sin5x / \sin(5x+2x) = \sin3x/\cos3x$$

$$(\cos5x \cdot \cos2x - \sin2x \cdot \sin5x) / \sin7x = \sin3x/\cos3x$$

$$\cos(5x+2x) / \sin7x = \sin3x/\cos3x$$

$$\cos7x / \sin7x - \sin3x / \cos3x = 0$$

$$(\cos7x \cdot \cos3x - \sin3x \cdot \sin7x) / \sin7x \cdot \cos3x = 0$$

$$\cos(7x+3x) / \sin7x \cdot \cos3x = 0$$

$$\cos10x = 0$$

$$10x = P/2 + Pn$$

$$x = P/20 + Pk/10$$

$$\cos5x \neq 0$$

$$5x \neq P/2 + Pn$$

$$x \neq P/10 + Pn/5$$

$$\cos2x \neq 0$$

$$2x \neq P/2 + Pn$$

$$x \neq P/4 + Pn/2$$

$$\sin5x \neq 0$$

$$5x \neq Pn$$

$$x \neq Pn/5$$

$$\sin2x \neq 0$$

$$2x \neq Pn$$

$$x \neq Pn/2$$

$$\cos3x \neq 0$$

$$3x \neq P/2 + Pn$$

$$x \neq P/6 + Pn/3$$

$$P/20 + Pk/10 = P/10 + Pn/5$$

$$1/20 + k/10 = 1/10 + n/5$$

$$1 + 2k = 2 + 4n$$

$$4n - 2k = -1$$

$$2(2n - k) = -1$$

Решений нет

$$P/20 + Pk/10 = P/4 + Pn/2$$

$$1/20 + k/10 = 1/4 + n/2$$

$$1 + 2k = 5 + 10n$$

$$10n - 2k = -4$$

$$2(5n - k) = -4$$

$$5n - k = -2$$

$$n = -1$$

$$k = -3$$

$$n = -1 + (-1) \cdot t$$

$$k = -3 - 5 \cdot t$$

$$k! = -3 - 5 \cdot t$$

$$P/20 + Pk/10 = Pn/5$$

$$1/20 + k/10 = n/5$$

$$1 + 2k = 4n$$

$$2(2n - k) = -1$$

Решений нет

$$P/20 + Pk/10 = Pn/2$$

$$1/20 + k/10 = n/2$$

$$1 + 2k = 10n$$

$$2(5n - k) = -1$$

Решений нет

$$P/20 + Pk/10 = P/6 + Pn/3$$

$$1/20 + k/10 = 1/6 + n/3$$

$$3 + 6k = 10 + 20n$$

$$2(10n - 3k) = -7$$

Решений нет

Ответ: $P/20 + Pk/10$, где k - любое целое, кроме $-3 - 5 \cdot t$, где t - произвольное целое