

$$4\operatorname{tg}3y = 3\operatorname{tg}2x$$
$$2\sin x \cdot \cos(x-y) = \sin y$$

$$4\operatorname{tg}(2y+y) = 3\operatorname{tg}2x$$
$$4(\operatorname{tg}2y + \operatorname{tgy}) / (1 - \operatorname{tg}2y\operatorname{tgy}) = 3\operatorname{tg}2x$$

$$2\sin x \cdot \cos(x-y) = \sin y$$
$$2\sin x (\cos x \cdot \cos y + \sin y \cdot \sin x) = \sin y$$
$$2\sin x \cos x \cos y + 2\sin^2 x \sin y = \sin y$$

$$\sin 2x \cos y - \cos 2x \sin y + \sin y = \sin y$$
$$\sin 2x \cos y - \cos 2x \sin y = 0$$
$$\sin(2x-y) = 0$$
$$2x-y = \pi k$$
$$2x = \pi k + y$$

$$\operatorname{tg}2x = \operatorname{tg}(\pi k + y)$$
$$\operatorname{tg}2x = \operatorname{tgy}$$
$$4(\operatorname{tg}2y + \operatorname{tgy}) / (1 - \operatorname{tg}2y\operatorname{tgy}) = 3\operatorname{tgy}$$
$$4(2\operatorname{tgy} / (1 - \operatorname{tg}^2 y) + \operatorname{tgy}) / (1 - 2\operatorname{tgy}\operatorname{tgy} / (1 - \operatorname{tg}^2 y)) = 3\operatorname{tgy}$$
$$\operatorname{tgy} = t$$
$$4(2t / (1 - t^2) + t) / (1 - 2t^2 / (1 - t^2)) = 3t$$
$$4((2t + t - t^3) / (1 - t^2)) / ((1 - t^2 - 2t^2) / (1 - t^2)) = 3t$$
$$4((3t - t^3) / (1 - t^2)) / ((1 - 3t^2) / (1 - t^2)) = 3t$$
$$(12t - 4t^3) / (1 - t^2) \cdot (1 - t^2) / (1 - 3t^2) = 3t$$
$$(12t - 4t^3) / (1 - 3t^2) = 3t$$
$$(12t - 4t^3 - 3t + 9t^3) / (1 - 3t^2) = 0$$
$$5t^3 + 9t = 0$$
$$t(5t^2 + 9) = 0$$
$$t = 0$$
$$\operatorname{tgy} = 0$$

$$y = \pi n$$
$$x = (\pi k + \pi n) / 2$$

Ответ:  $((\pi k + \pi n) / 2; \pi k)$

$$\operatorname{tg}2x = \sin 2x / \cos 2x = 2\sin x \cos x / (1 - 2\sin^2 x) = 2\operatorname{tg}x / (1 + \operatorname{tg}^2 x - 2\operatorname{tg}^2 x) =$$
$$2\operatorname{tg}x / (1 - \operatorname{tg}^2 x)$$
$$\operatorname{tg}(x+y) = \sin(x+y) / \cos(x+y) = (\sin x \cos y + \sin y \cos x) / (\cos x \cos y - \sin y \sin x) =$$
$$= (\operatorname{tg}x + \operatorname{tgy}) / (1 - \operatorname{tg}x\operatorname{tgy})$$