

$$2\cos 2x + \sin 2x \geq \tan x$$

$$2(1-\tan^2 x)/(1+\tan^2 x) + 2\tan x/(1+\tan^2 x) \geq \tan x$$
$$\tan x = t$$

$$2(1-t^2)/(1+t^2) + 2t/(1+t^2) \geq t$$

$$2-2t^2+2t \geq t+t^3$$

$$t^3+2t^2-t-2 \leq 0$$

$$t^2(t+2)-(t+2) \leq 0$$

$$(t^2-1)(t+2) \leq 0$$

$$t = -1$$

$$t = -2$$

$$t \in (-\infty; -2] \cup [-1; 1]$$

$$\tan x \leq -2$$

$$-\pi/2 + p\pi < x \leq \arctan(-2) + p\pi$$

$$-1 \leq \tan x \leq 1$$

$$-\pi/4 + p\pi \leq x \leq \pi/4 + p\pi$$

$$\sin^2 x = \sin^2 x / 1 = \sin^2 x / (\sin^2 x + \cos^2 x) = \tan^2 x / (1 + \tan^2 x)$$
$$\cos^2 x = \cos^2 x / (\cos^2 x + \sin^2 x) = 1 / (1 + \tan^2 x)$$
$$\sin 2x = \sin 2x / 1 = \sin 2x / (\cos^2 x + \sin^2 x) = 2 \sin x \cos x / (\cos^2 x + \sin^2 x) = 2 \tan x / (1 + \tan^2 x)$$
$$\cos 2x = \cos 2x / 1 = (\cos^2 x - \sin^2 x) / (\cos^2 x + \sin^2 x) = (1 - \tan^2 x) / (1 + \tan^2 x)$$

