

$\sin(\text{arctg}x)=?$
 $\text{arctg}x = t \in (0;P)$
 $1/\sin^2t=1+\text{ctg}^2t$
 $\sin t = \pm\sqrt{1/(1+\text{ctg}^2x)} = \pm\sqrt{1/(1+x^2)}$
 $\sin t = \sqrt{1/(1+x^2)}$

$\cos(\arcsinx)=?$
 $\arcsinx = t \in [-P/2;P/2]$
 $\cos t = \pm\sqrt{1-\sin^2t} = \pm\sqrt{1-x^2}$
 $\cos t = \sqrt{1-x^2}$

$\cos(\text{arctg}x)=?$
 $\text{arctg}x = t \in (-P/2;P/2)$
 $\text{tgt} = x$
 $1+\text{tg}^2x = 1/\cos^2x$
 $\cos t = \pm\sqrt{1/(1+\text{tg}^2t)} = \pm\sqrt{1/(1+x^2)}$
 $\cos t = \sqrt{1/(1+x^2)}$

$\cos(\text{arcctg}x)=?$
 $\text{arcctg}x = t \in (0;P)$
 $\text{ctgt} = x$
 $\text{tgt} = 1/x$
 $\cos t = \pm\sqrt{1/(1+\text{tg}^2t)} = \pm\sqrt{1/(1+1/x^2)} = \pm\sqrt{x^2/(x^2+1)}$
 при $t \in (0;P/2)$ $\cos t > 0$ $\cos t = \sqrt{x^2/(x^2+1)} = |x|/\sqrt{x^2+1} = x/\sqrt{x^2+1}$
 при $t \in [P/2;P)$ $\cos t < 0$ $\cos t = -\sqrt{x^2/(x^2+1)} = -|x|/\sqrt{x^2+1} = -x/\sqrt{x^2+1}$

$\text{tg}(\arcsinx)=?$
 $\arcsinx = t \in [-P/2;P/2]$
 $\sin t = x$
 $1+1/\text{tg}^2t = 1/\sin^2t$
 $\text{tg}^2t = 1/(1/\sin^2t - 1) = \sin^2t/(1-\sin^2t)$
 $\text{tgt} = \pm\sqrt{\sin^2t/(1-\sin^2t)} = \pm\sqrt{x^2/(1-x^2)}$
 при $t \in [-P/2;0]$ $\text{tgt} < 0$ $\text{tgt} = -\sqrt{x^2/(1-x^2)} = -|x|/\sqrt{1-x^2} = -x/\sqrt{1-x^2}$
 при $t \in (0;P/2]$ $\text{tgt} > 0$ $\text{tgt} = \sqrt{x^2/(1-x^2)} = |x|/\sqrt{1-x^2} = x/\sqrt{1-x^2}$

$\text{tg}(\arccosx)=?$
 $\arccosx = t \in [0;P]$
 $\cos t = x$
 $\text{tgt} = \pm\sqrt{1/\cos^2t - 1} = \pm\sqrt{(1-\cos^2t)/\cos^2t}$
 $\text{tgt} = \sqrt{(1-x^2)/x^2}$
 при $t \in [0;P/2]$ $\text{tgt} > 0$ $\text{tgt} = \sqrt{(1-x^2)/x^2} = \sqrt{1-x^2}/|x| = \sqrt{1-x^2}/x$
 при $t \in (P/2;P]$ $\text{tgt} < 0$ $\text{tgt} = -\sqrt{(1-x^2)/x^2} = -\sqrt{1-x^2}/|x| = -\sqrt{1-x^2}/x$

$\text{tg}(\text{arcctg}x)=?$
 $\text{arcctg}x = t \in (0;P)$
 $\text{ctgt} = x$
 $\text{tgt} = 1/\text{ctgt} = 1/x$

$\text{ctg}(\arcsinx)=?$
 $\arcsinx = t \in [-P/2;P/2]$
 $\sin t = x$
 $\text{ctgt} = \pm\sqrt{(1-\sin^2t)/|\sin t|}$
 при $t \in [-P/2;0]$ $\text{ctgt} < 0$ $\text{ctgt} = -\sqrt{(1-\sin^2t)/|\sin t|} = -\sqrt{(1-x^2)/|x|} = \sqrt{1-x^2}/x$
 при $t \in [0;P/2]$ $\text{ctgt} > 0$ $\text{ctgt} = \sqrt{(1-\sin^2t)/|\sin t|} = \sqrt{(1-x^2)/|x|} = \sqrt{1-x^2}/x$

$\text{ctg}(\arccosx)=?$
 $\arccosx = t \in [0;P]$
 $\cos t = x$
 $1/\text{ctg}^2t = 1/\cos^2t - 1 = (1-\cos^2t)/\cos^2t$
 $\text{ctgt} = \pm\sqrt{|\cos t|/\sqrt{1-\cos^2t}} = \pm\sqrt{|x|/\sqrt{1-x^2}}$
 при $t \in [0;P/2]$ $\text{ctgt} > 0$ $\text{ctgt} = |x|/\sqrt{1-x^2} = x/\sqrt{1-x^2}$
 при $t \in [P/2;P]$ $\text{ctgt} < 0$ $\text{ctgt} = -|x|/\sqrt{1-x^2} = -x/\sqrt{1-x^2}$

$\text{ctg}(\text{arctg}x)=?$
 $\text{arctg}x = t \in (-P/2;P/2)$
 $\text{tgt} = x$
 $\text{ctgt} = 1/\text{tgt} = 1/x$