

АРКИ УРАВНЕНИЯ 08

$$\arcsinx * \arccosx = -1$$

$$\arcsinx \in [-\pi/2; \pi/2]$$

$$\arccosx \in [0; \pi]$$

$$-1 \leq x \leq 1$$

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$$(\pi/2 - \arccosx) \arccosx = -1$$

$$\pi/2 \arccosx - \arccos^2 x + 1 = 0$$

$$\arccosx = t$$

$$-t^2 + \pi/2t + 1 = 0$$

$$t^2 - \pi/2t - 1 = 0$$

$$D = \pi^2/4 + 4 = (\pi^2 + 16)/4$$

$$t = (\pi/2 + \sqrt{(\pi^2 + 16)/2})/2 = \pi/4 + \sqrt{(\pi^2 + 16)/4} =$$

$$(\pi + \sqrt{\pi^2 + 16})/4$$

$$t = (\pi - \sqrt{\pi^2 + 16})/4$$

$$\arccosx \in [0; \pi]$$

$$\arccosx = (\pi + \sqrt{\pi^2 + 16})/4 \text{ -- подходит}$$

$$\arccosx = (\pi - \sqrt{\pi^2 + 16})/4 \text{ -- отриц -- не}$$

подходит

$$\arccosx = (\pi + \sqrt{\pi^2 + 16})/4 \setminus \cos$$

$$x = \cos((\pi + \sqrt{\pi^2 + 16})/4)$$

$$\begin{aligned} \sqrt{1-\cos x} &= \sin x \\ \cos x - \sin x &= \sqrt{2}\sin(x + 3\pi/4) \\ \sqrt{2}\sin(x + 3\pi/4) &\geq 0 \\ \sin(x + 3\pi/4) &\geq 0 \\ 2k\pi &\leq x + 3\pi/4 \leq \pi + 2k\pi \\ 2k\pi - 3\pi/4 &\leq x \leq \pi/4 + 2k\pi \end{aligned}$$

$$1 - \cos x = \sin^2 x - 2\sin x \cos x + \cos^2 x$$

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$$1 - \cos x = 1 - 2\sin x \cos x$$

$$\cos x = 2\sin x \cos x$$

$$\cos x - 2\sin x \cos x = 0$$

$$\cos x(1/\sin x - 2\sin x) = 0$$

$$\cos x = 0$$

$$x = \pi/2 + k\pi$$

$$1/\sin x - 2\sin x = 0$$

$$1 - 2\sin^2 x = 0$$

$$\sin x \neq 0$$

$$1 - (1 - \cos 2x) = 0$$

$$\cos 2x = 0$$

$$2x = \pi/2 + k\pi$$

$$x = \pi/4 + k\pi/2$$

Ответ $x = \pi/4 + k\pi; -\pi/2 + k\pi; -\pi/4 + k\pi$.

$$\arcsinx * \arccosx = -1$$

$$\begin{aligned} \sqrt{S} &= g \\ S &\geq 0 \\ \sqrt{S} &= g^2 \end{aligned}$$

